

# **Defense trees for economic evaluation of security investments**

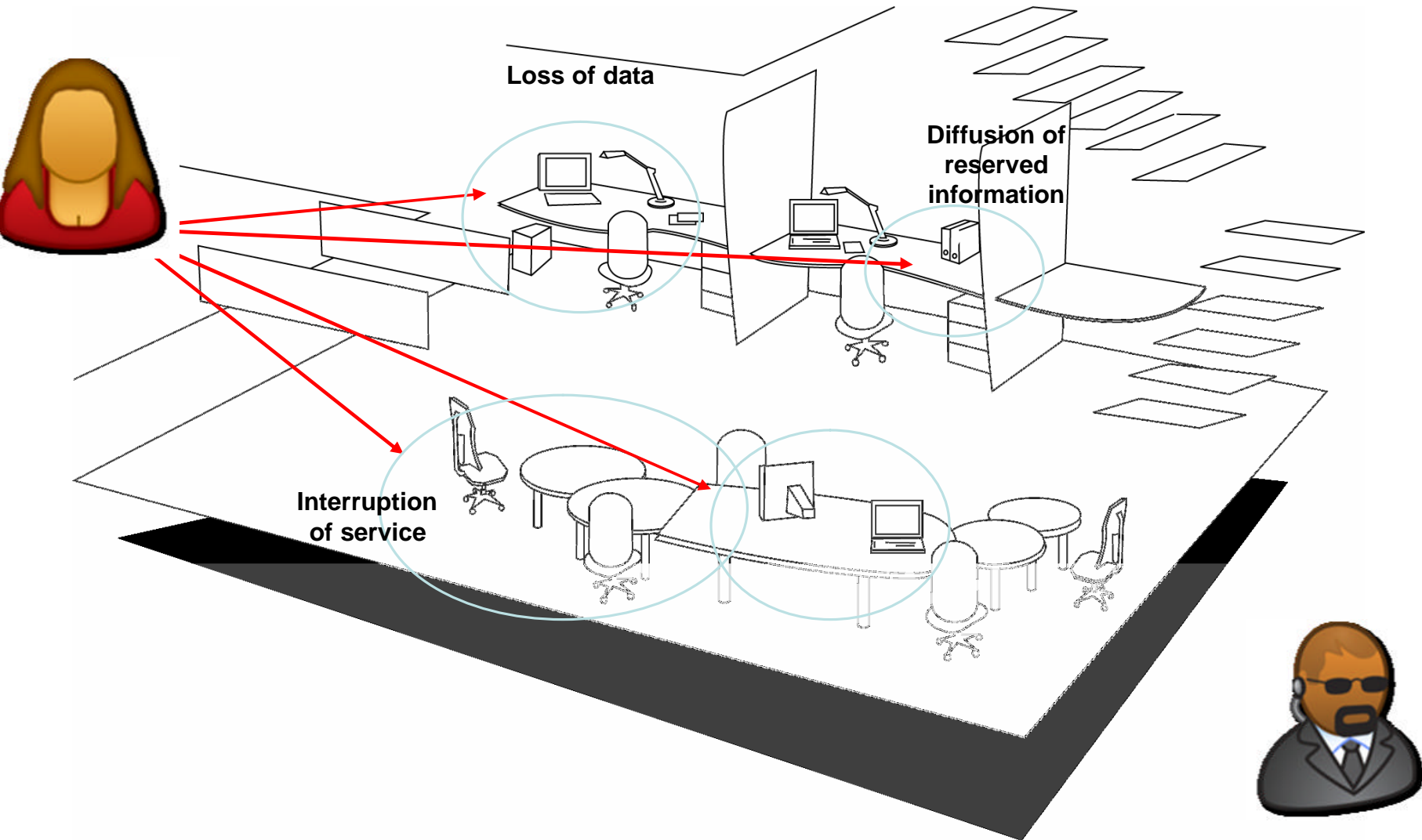
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# What is the problem?



**How to protect an organization's asset?**

# Motivation

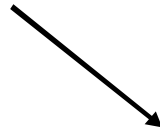
- + Create a *process* to identify, describe and analyze the possible vulnerabilities of a system
- + Provide an *economic balance* between the economic impact of risk and the cost of risk mitigation

# Agenda

## Background

- + Qualitative approach
  - + Attack trees
- + Quantitative approach
  - + Economic indexes

- + **Defense trees = Attack tree + countermeasures**
- + **Defense trees + quantitative labels**



**Economic evaluation  
of countermeasures**

# Qualitative approach

A relative evaluation of:

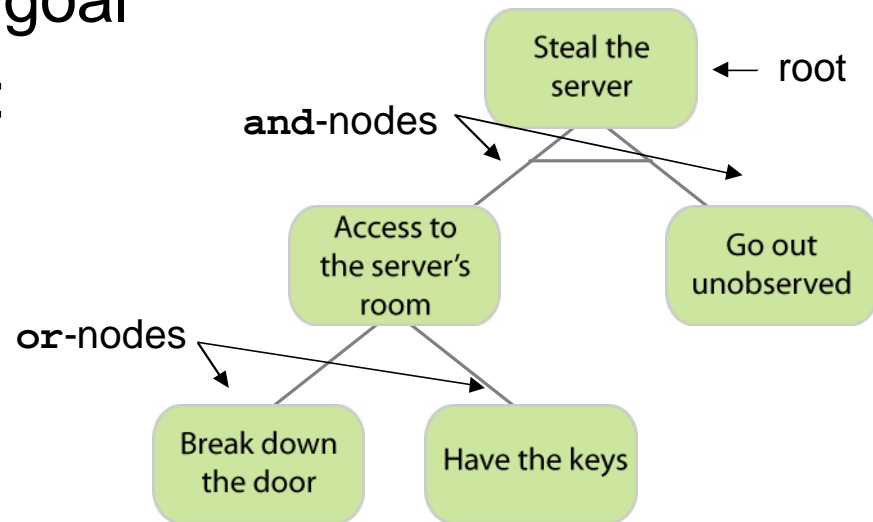
- + assets
- + threats and vulnerabilities
- + countermeasures

Scenario analysis → **Attack trees**

# Attack trees

An *attack tree* [Schneier00] is a tree-based structure where:

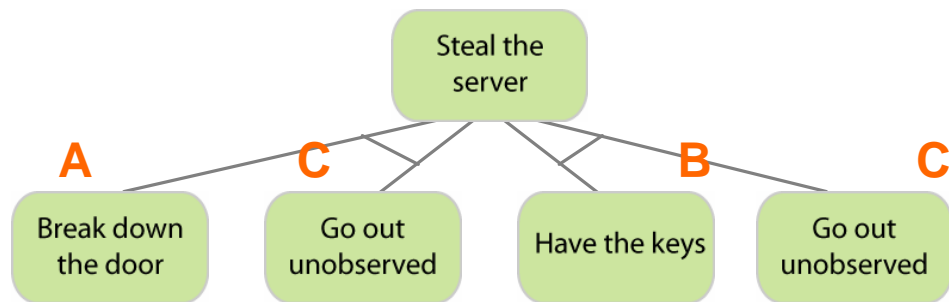
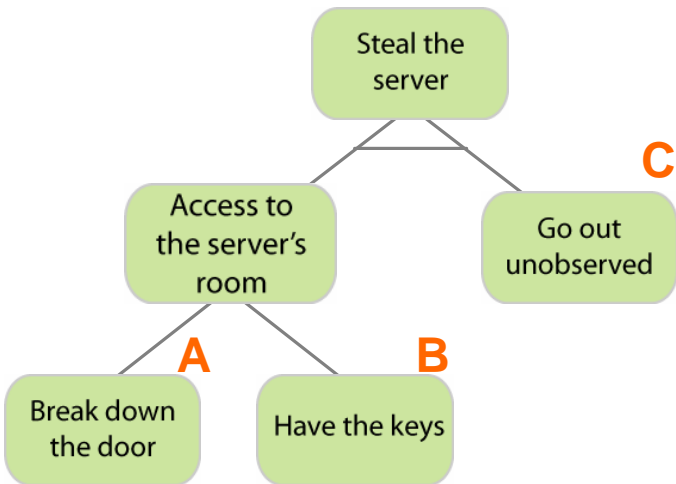
- + the root is an asset of an IT system
- + the paths from the root to the leaf are the way to achieve this goal
- + the non-leaf nodes can be:
  - + and-nodes
  - + or-nodes



# Attack trees

An attack tree can be transformed to its *Disjunctive Normal Form* [Mauw05]

$$((A \text{ or } B) \text{ and } C) = (A \text{ and } C) \text{ or } (B \text{ and } C)$$



# Quantitative approach

Assigns absolute numeric attribute values to:

- + assets (asset value)
- + threats and vulnerabilities (exposure factor, annualized rate of occurrence)
- + countermeasures (cost, risk mitigated)



**Economic Indexes**



# Economic Indexes

## Return on Investment (ROI)



a performance measure used to evaluate the efficiency of an investment

$$ROI = \frac{\textit{Gain from Investment} - \textit{Cost of Investment}}{\textit{Cost of Investment}}$$

# Agenda

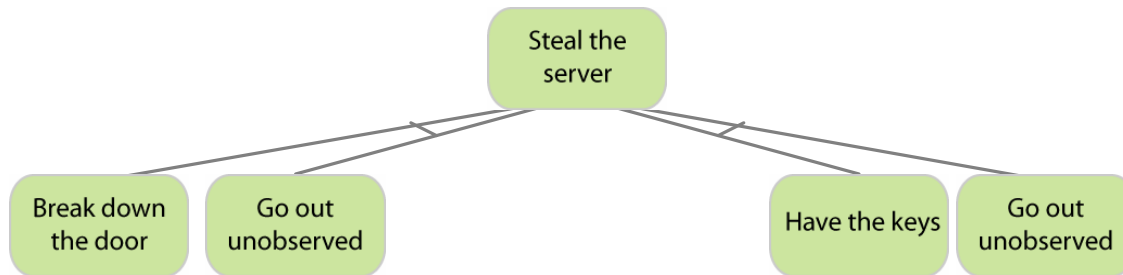
## Background

- + Qualitative approach
  - + Attack trees
- + Quantitative approach
  - + Economic indexes

- + **Defense trees = Attack tree + countermeasures**
- + **Defense trees + quantitative labels**

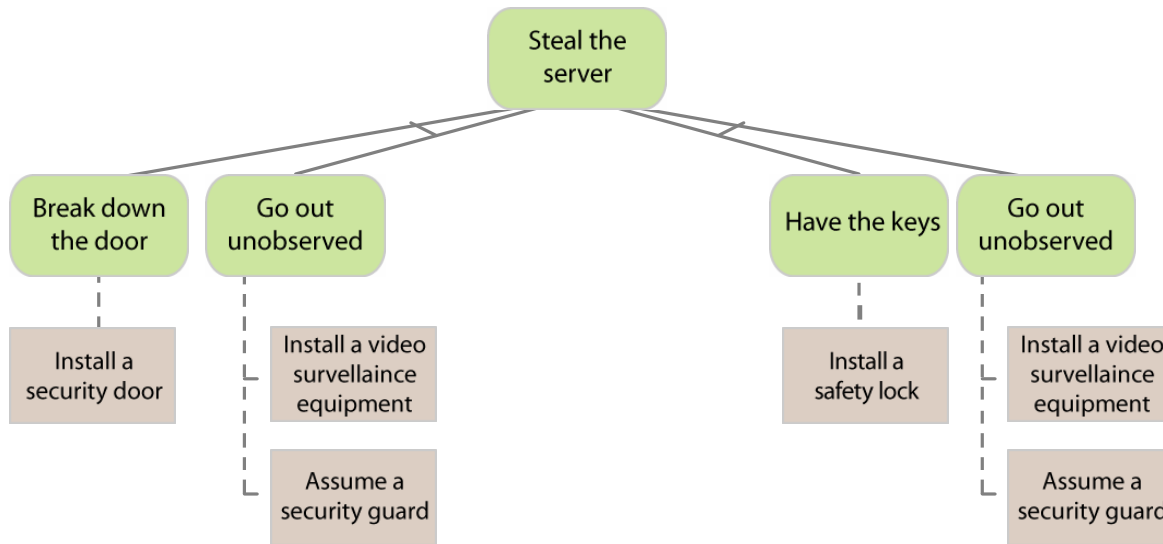
# Building the defense tree

1. Create an *attack tree*,



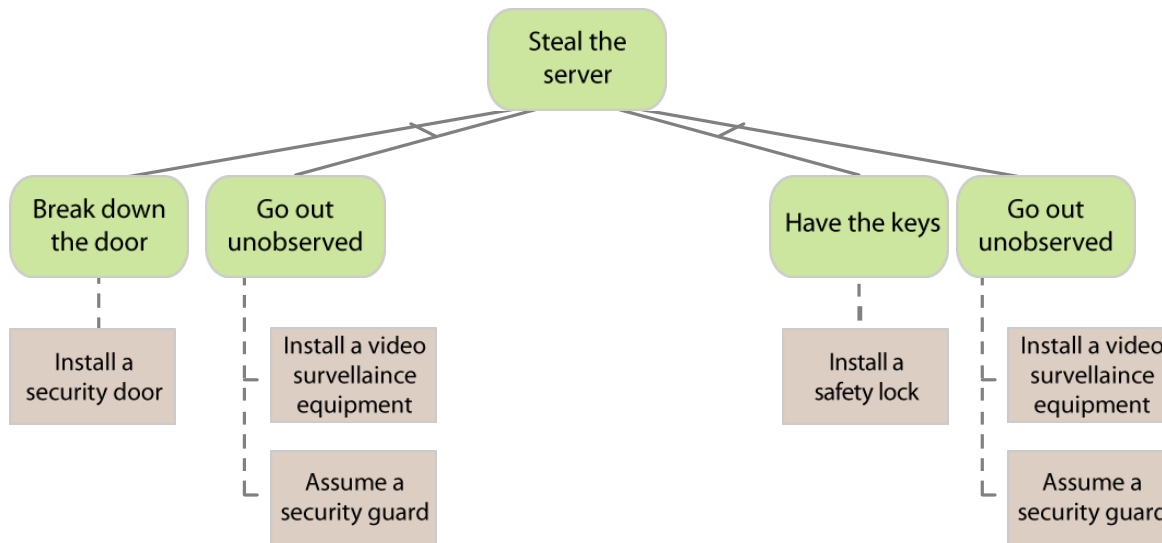
# Building the defense tree

2. *Defense tree* = attack tree + countermeasures



# Building the defense tree

3. Label the defense tree using quantitative indexes and computing the Return on Investment

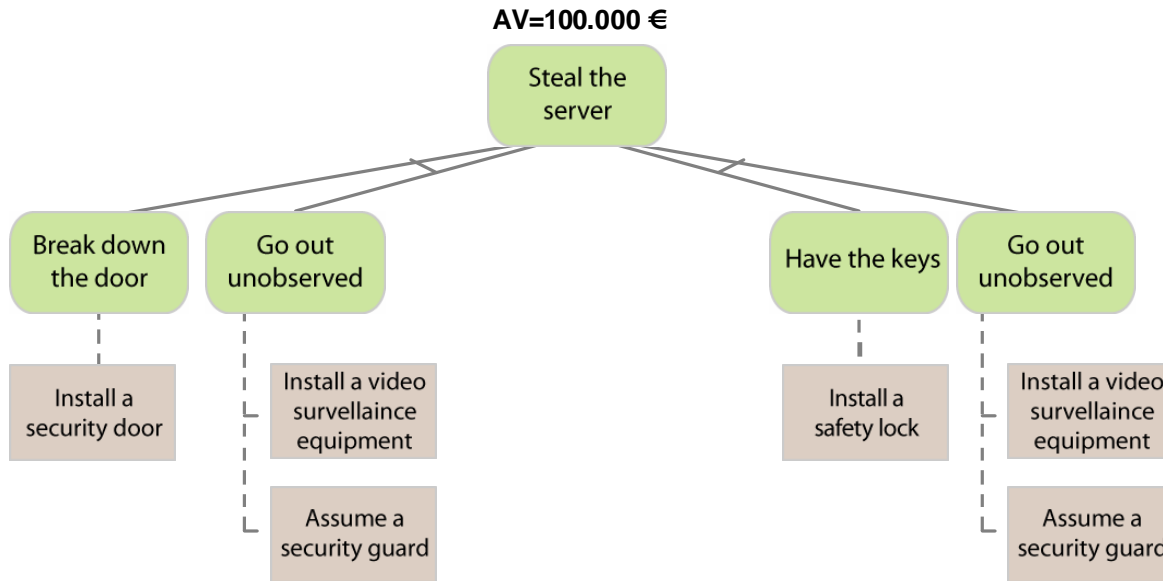


4. Label the defense tree using quantitative indexes and computing the Return on Attack [Cremonini05]



# Return On Investment

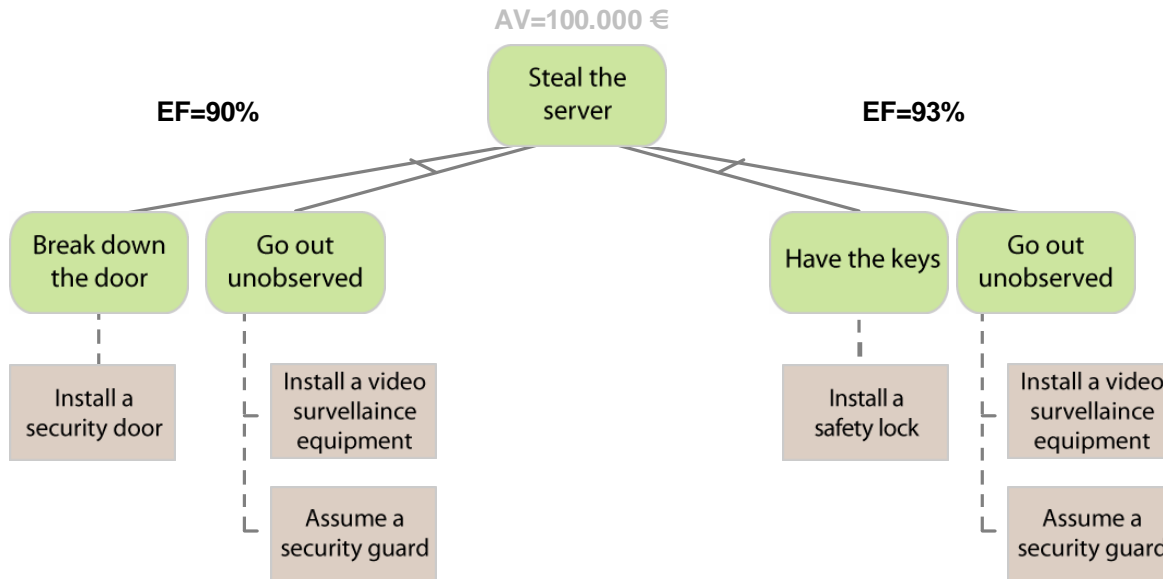
*Asset Value (AV)*



# Return On Investment

AV Asset Value

## Exposure Factor (EF)

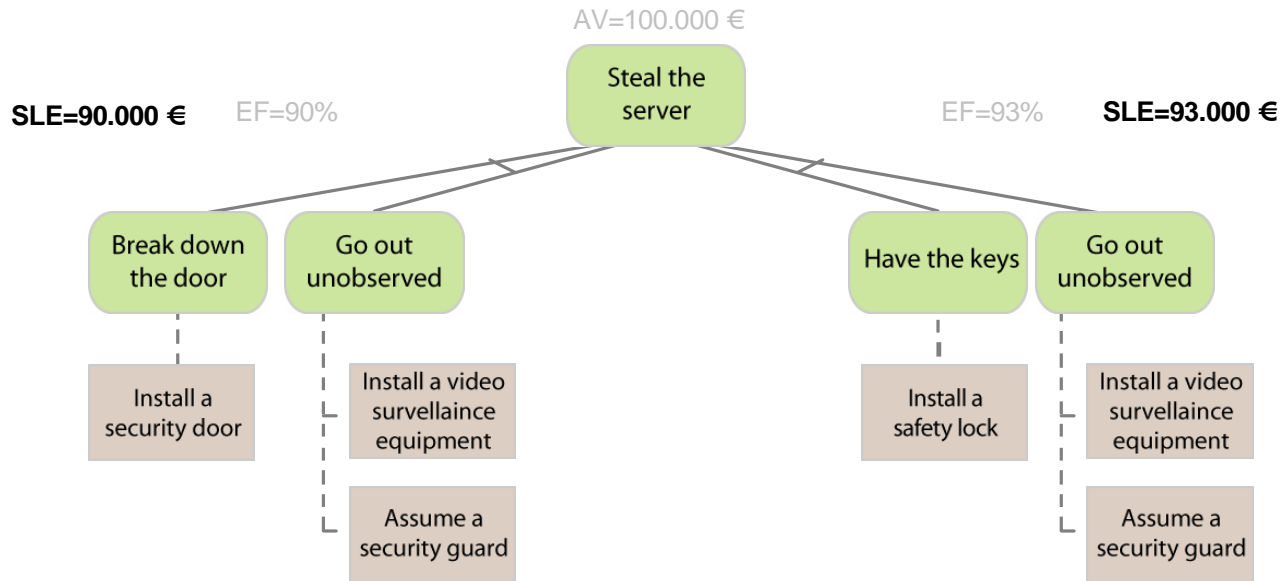


# Return On Investment

*Single Loss Exposure (SLE=AV × EF)*

**AV** Asset Value

**EF** Exposure Factor

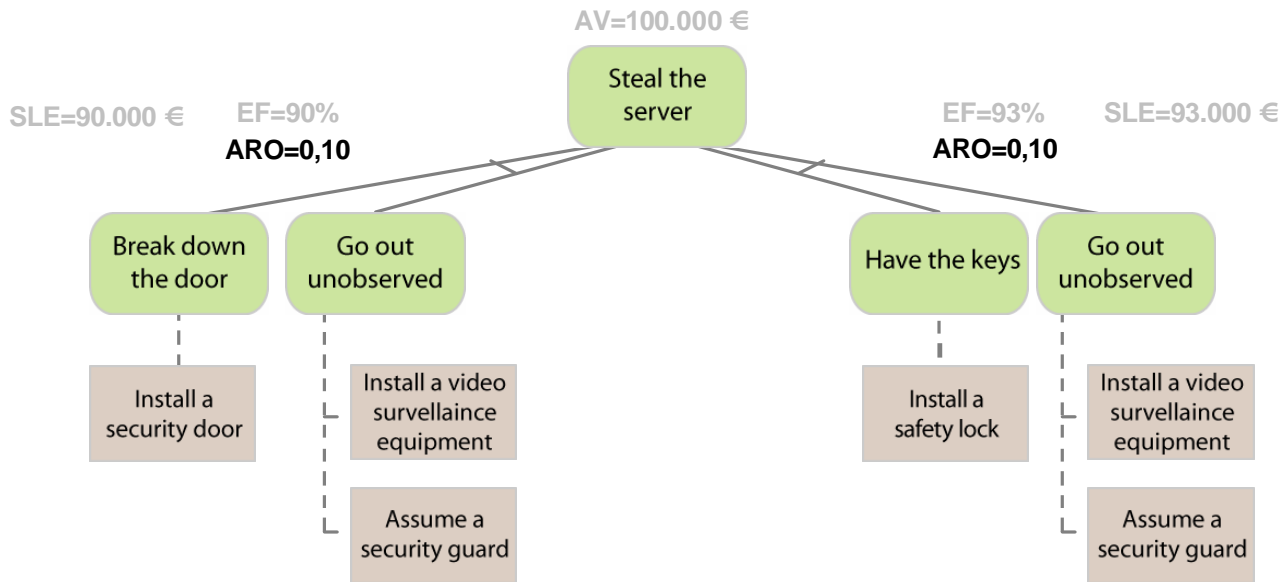




# Return On Investment

## Annualized Rate of Occurrence (ARO)

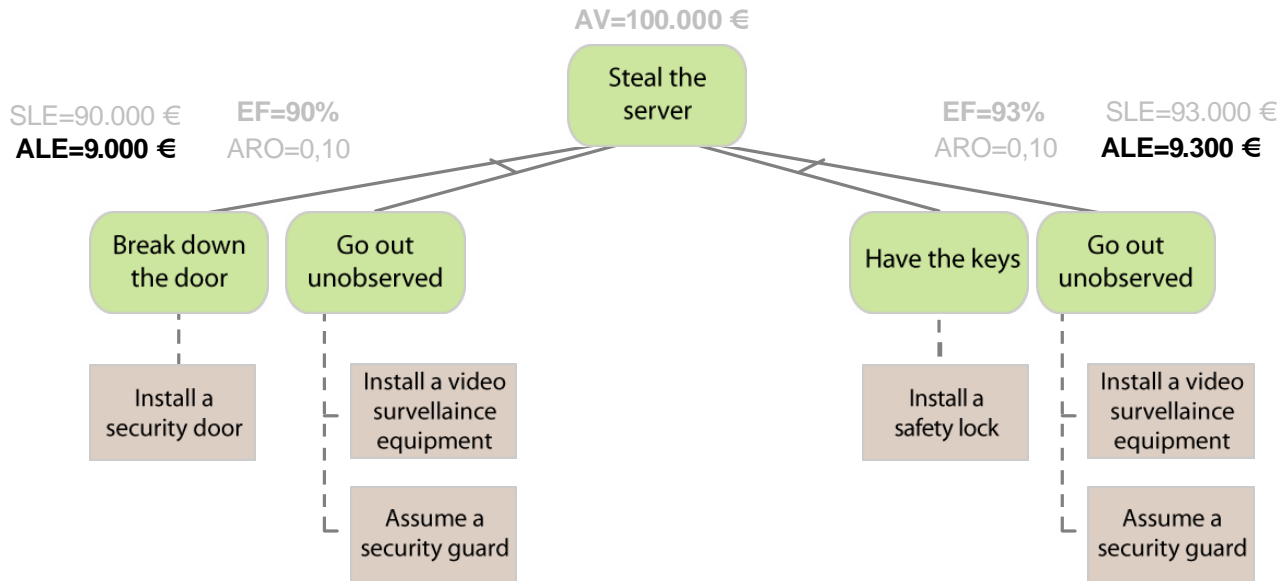
- AV** Asset Value
- EF** Exposure Factor
- SLE** Single Loss Exposure



# Return On Investment

*Annualized Loss Expectancy (ALE=SLE × ARO)*

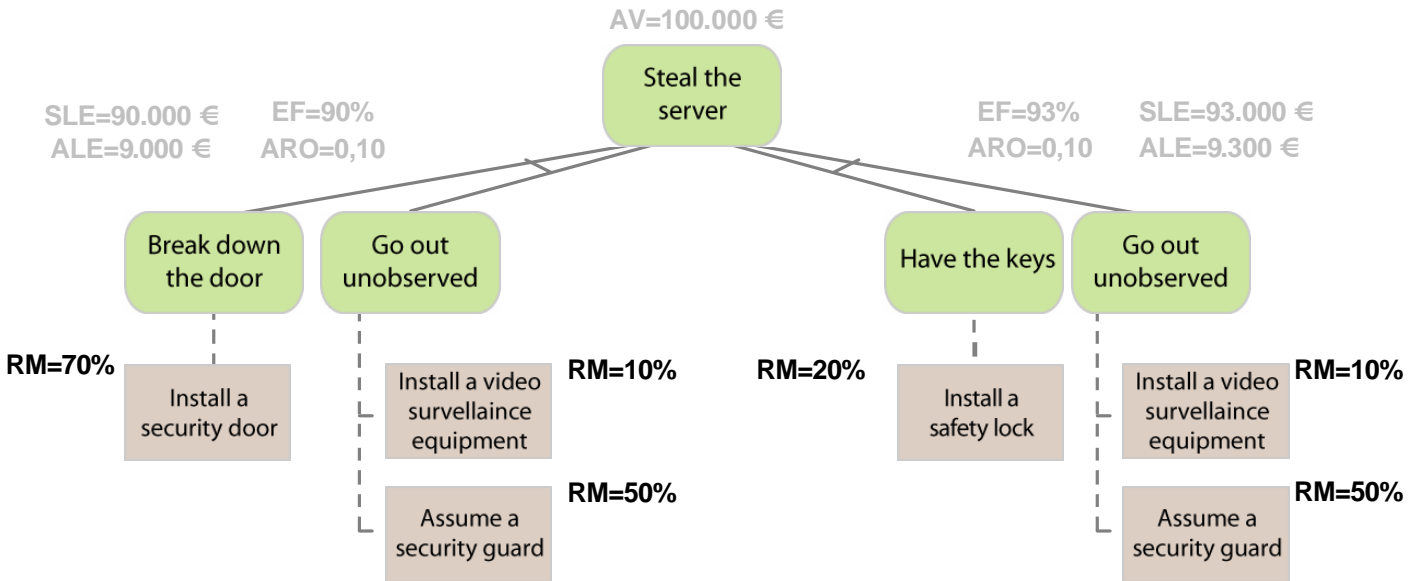
- AV** Asset Value
- EF** Exposure Factor
- SLE** Single Loss Exposure
- ARO** Annualized Rate of Occurrence



# Return On Investment

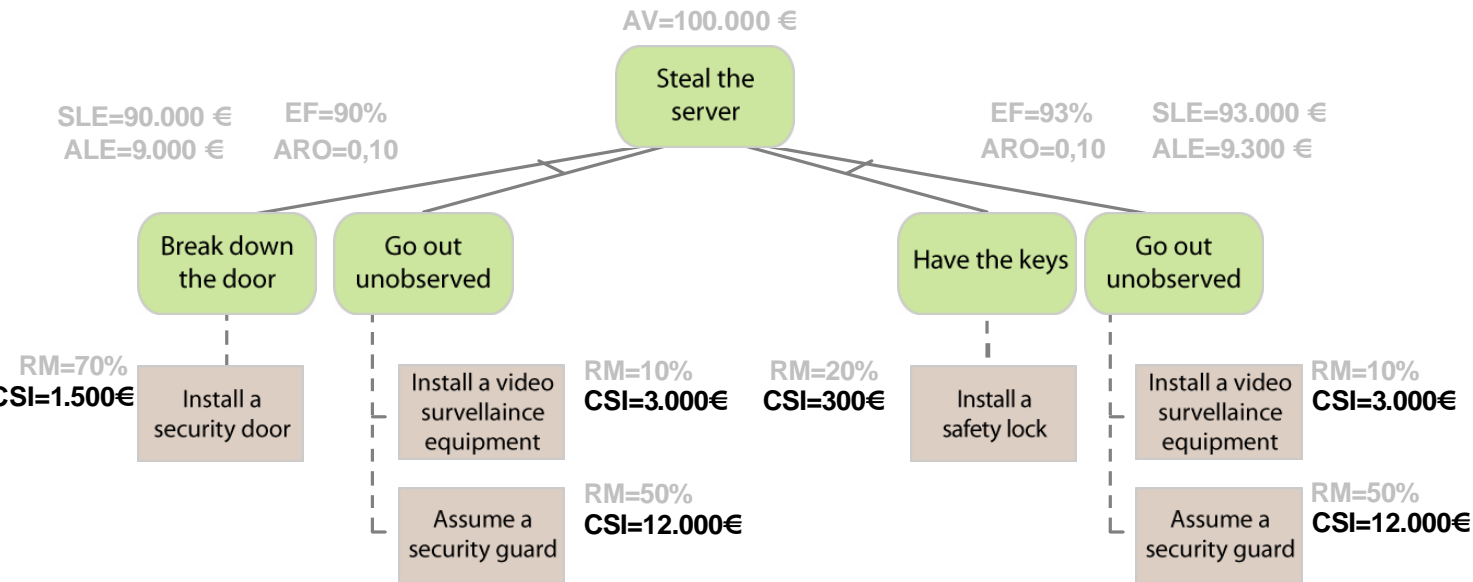
## Risk Mitigated by a countermeasure (RM)

- AV** Asset Value
- EF** Exposure Factor
- SLE** Single Loss Exposure
- ARO** Annualized Rate of Occurrence
- ALE** Annualized Loss Expectancy



# Return On Investment

## Cost of a Security Investment (CSI)



**AV** Asset Value

**EF** Exposure Factor

**SLE** Single Loss Exposure

**ARO** Annualized Rate of Occurrence

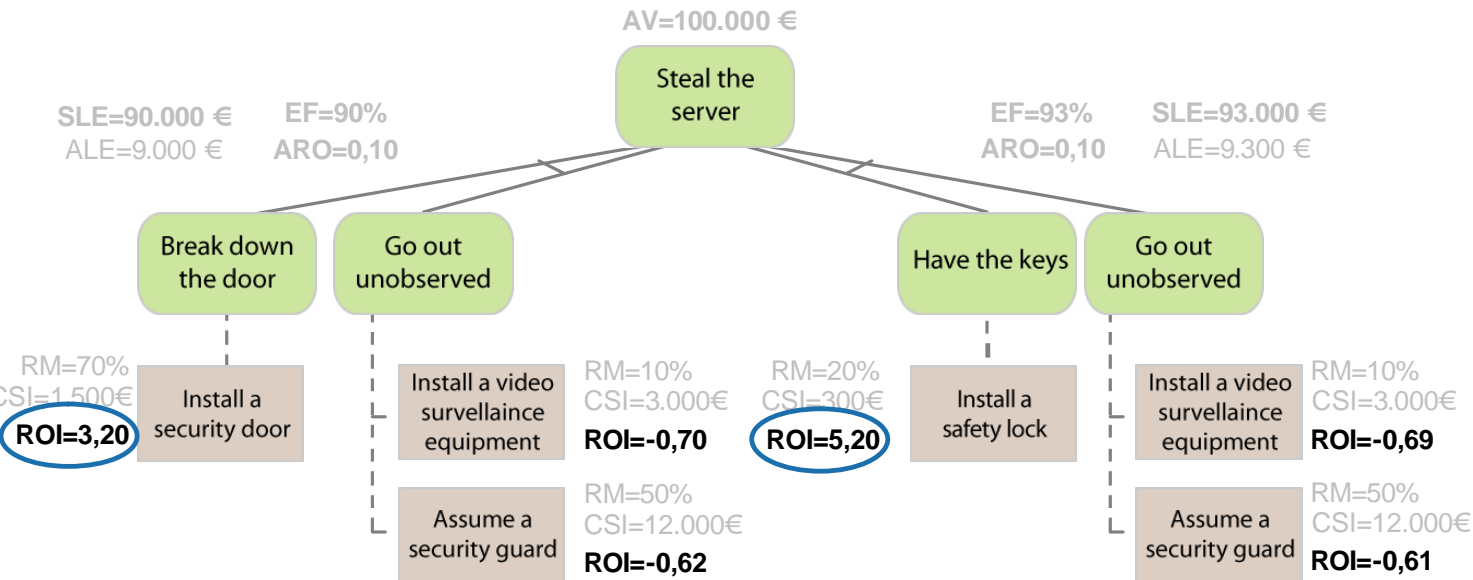
**ALE** Annualized Loss Expectancy

**RM** Risk Mitigated

# Return On Investment

$$ROI = \frac{(ALE \times RM) - CSI}{CSI}$$

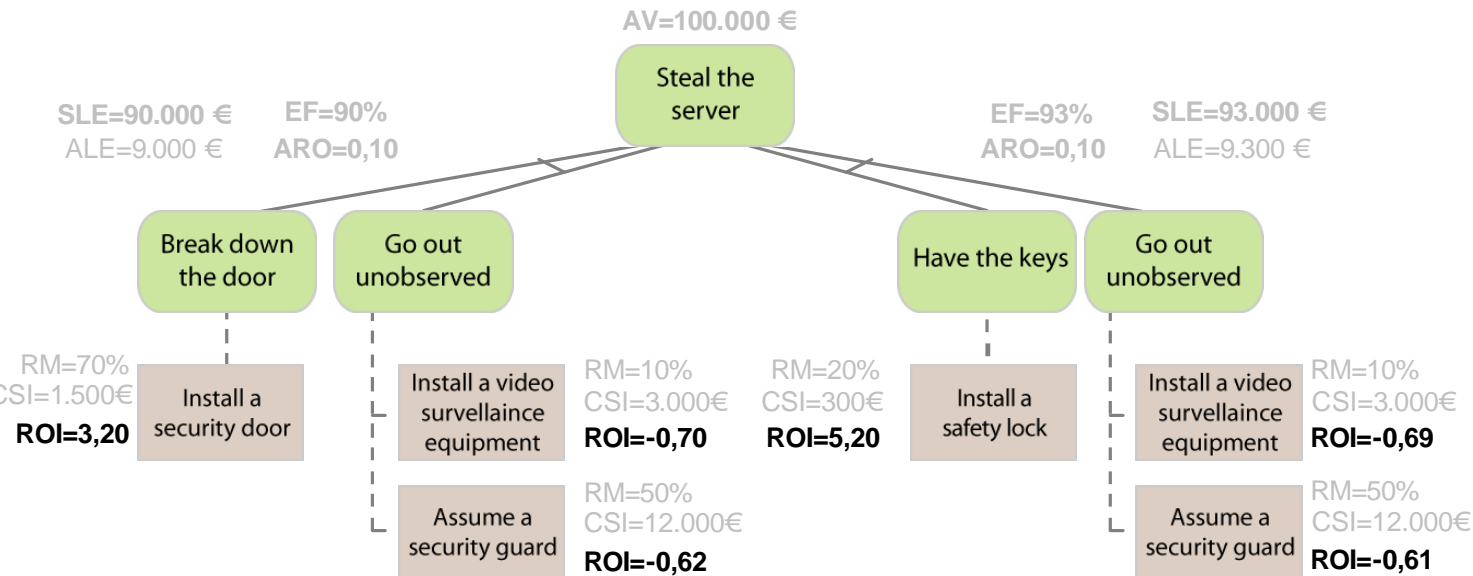
- AV** Asset Value
- EF** Exposure Factor
- SLE** Single Loss Exposure
- ARO** Annualized Rate of Occurrence
- ALE** Annualized Loss Expectancy
- RM** Risk Mitigated
- CSI** Cost Security Investment



# Risk F.W.

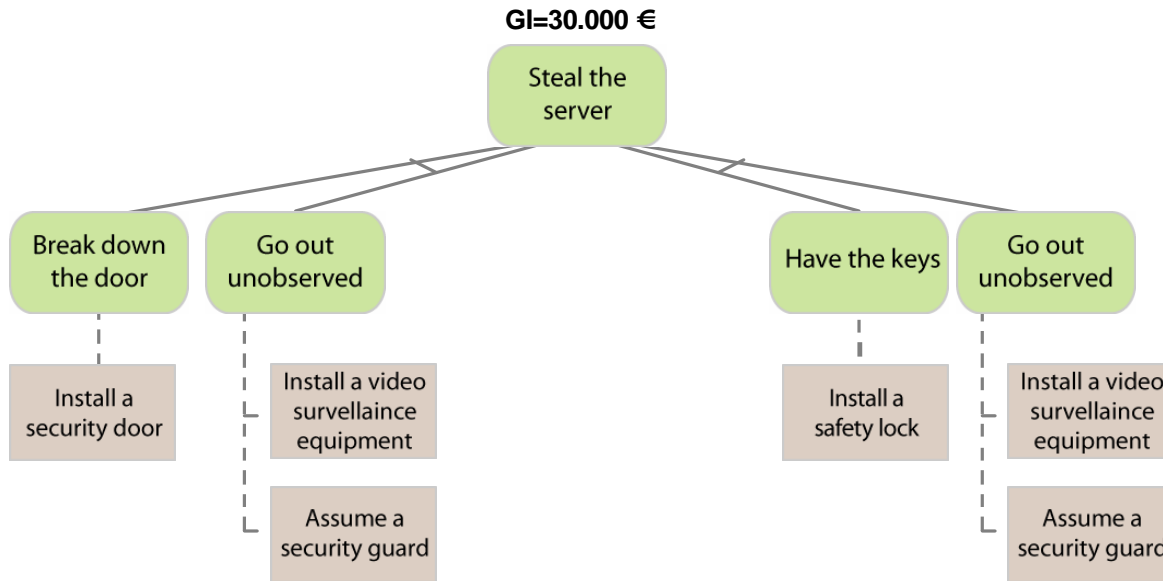
- + Consider **EF** as Uncertain variable with values in an interval ( $70 < \mathbf{EF} < 95$ ) (and similar for **RM**)
- + Compute ROI/ROA indexes as intervals
- + Study operations between intervals and notions of
  - + Optimistic combination
  - + Pessimistic combination
  - + Robustness
 (See works by Gervet-Yorke-Smith)

- AV** Asset Value
- EF** Exposure Factor
- SLE** Single Loss Exposure
- ARO** Annualized Rate of Occurrence
- ALE** Annualized Loss Expectancy
- RM** Risk Mitigated
- CSI** Cost Security Investment



# Return On Attack

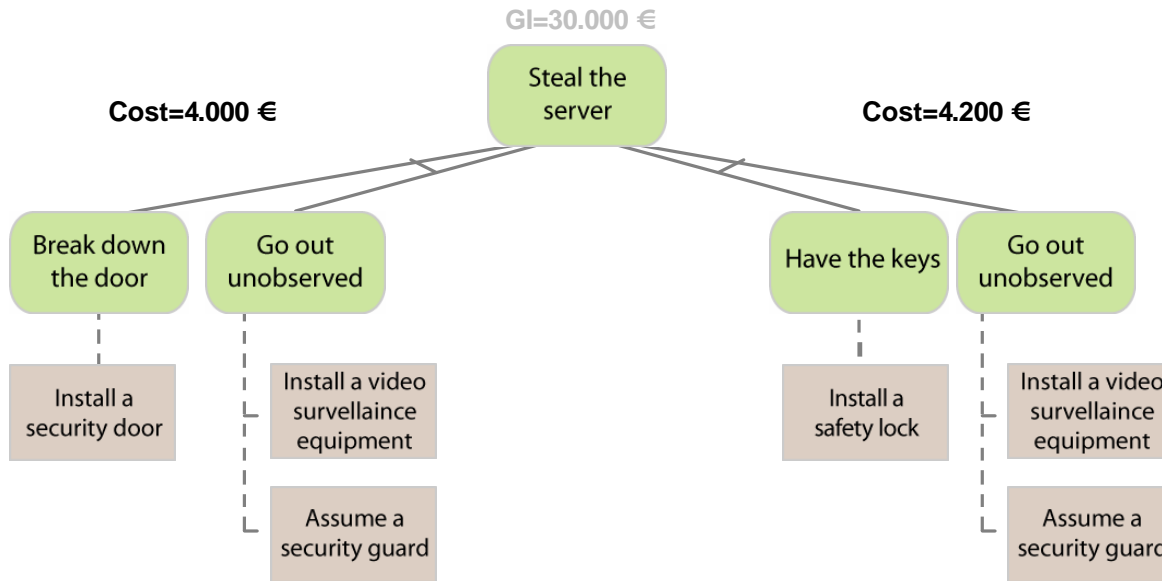
*Gain* that an attacker expects from an attack



# Return On Attack

GI expected gain

## Cost of an attack



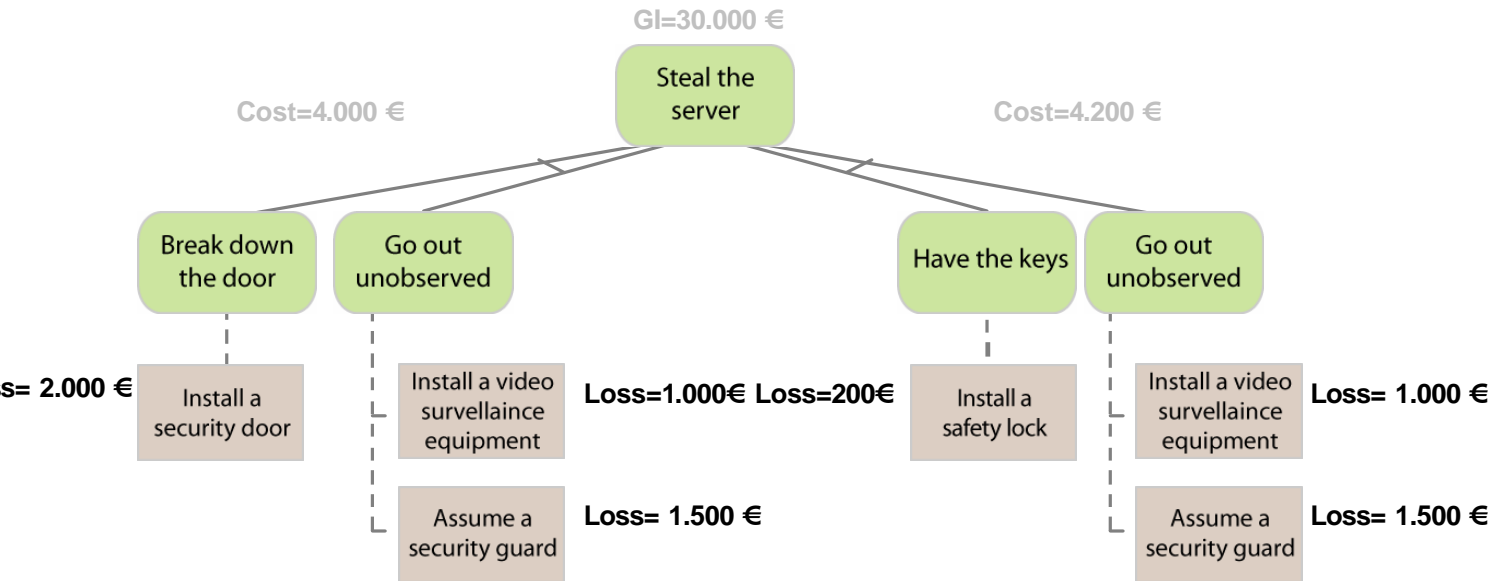


# Return On Attack

Additional cost (*loss*) caused by a countermeasure S

**GI** expected gain

**Cost** cost before S



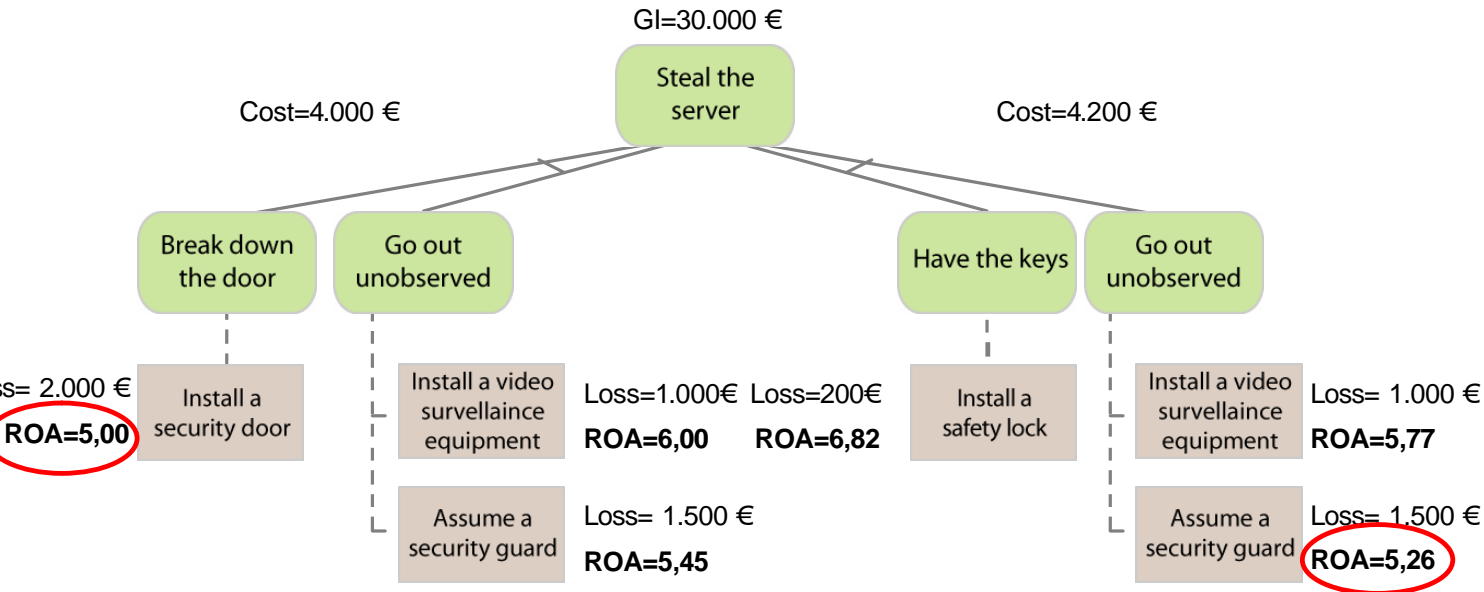
# Return On Attack

$$ROA = \frac{GI}{\text{cost before } S + \text{loss caused by } S}$$

**GI** expected gain

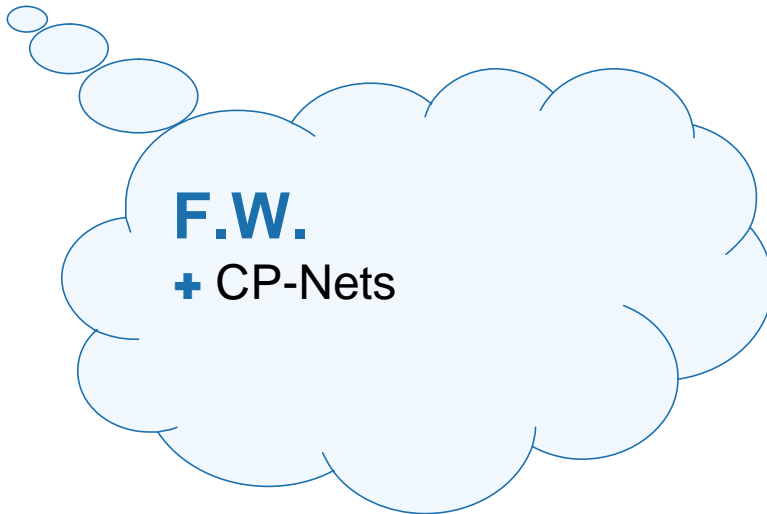
**Cost** cost before S

**Loss** loss caused by



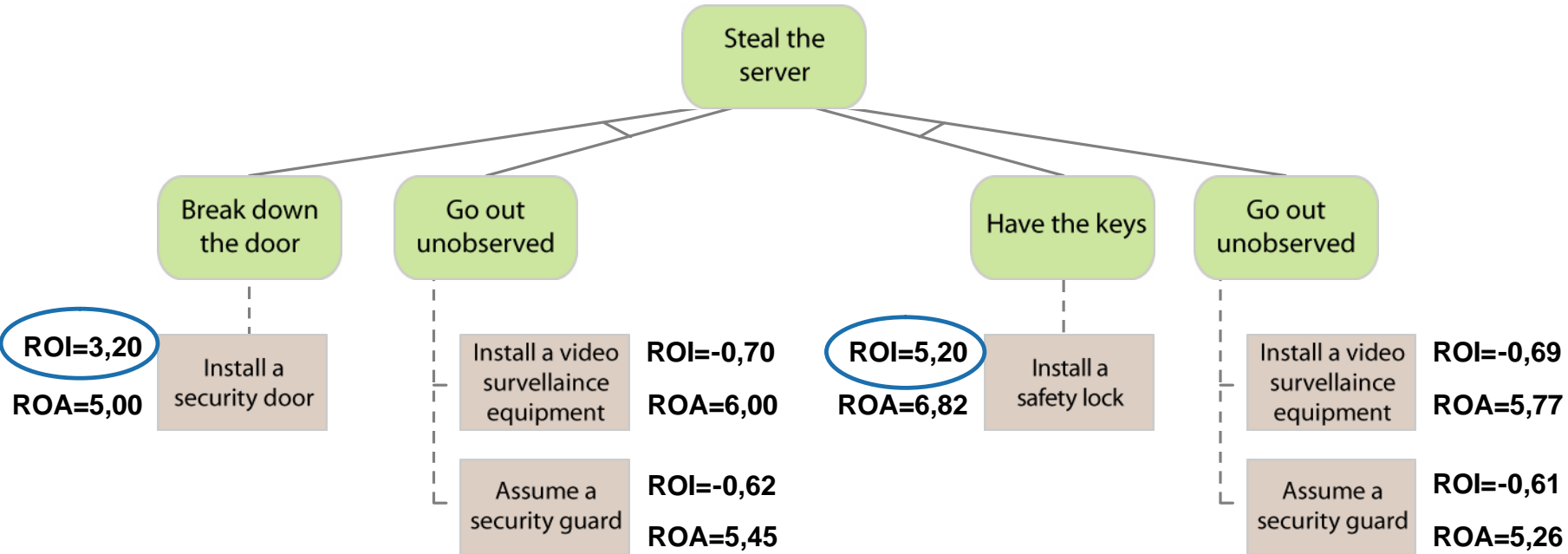
# Putting together the evaluations

- + Maximize ROI
- + minimize ROA
- + max ROI min ROA
- + a Pareto-optimal solution
- + maximize a user-defined function of ROI and ROA



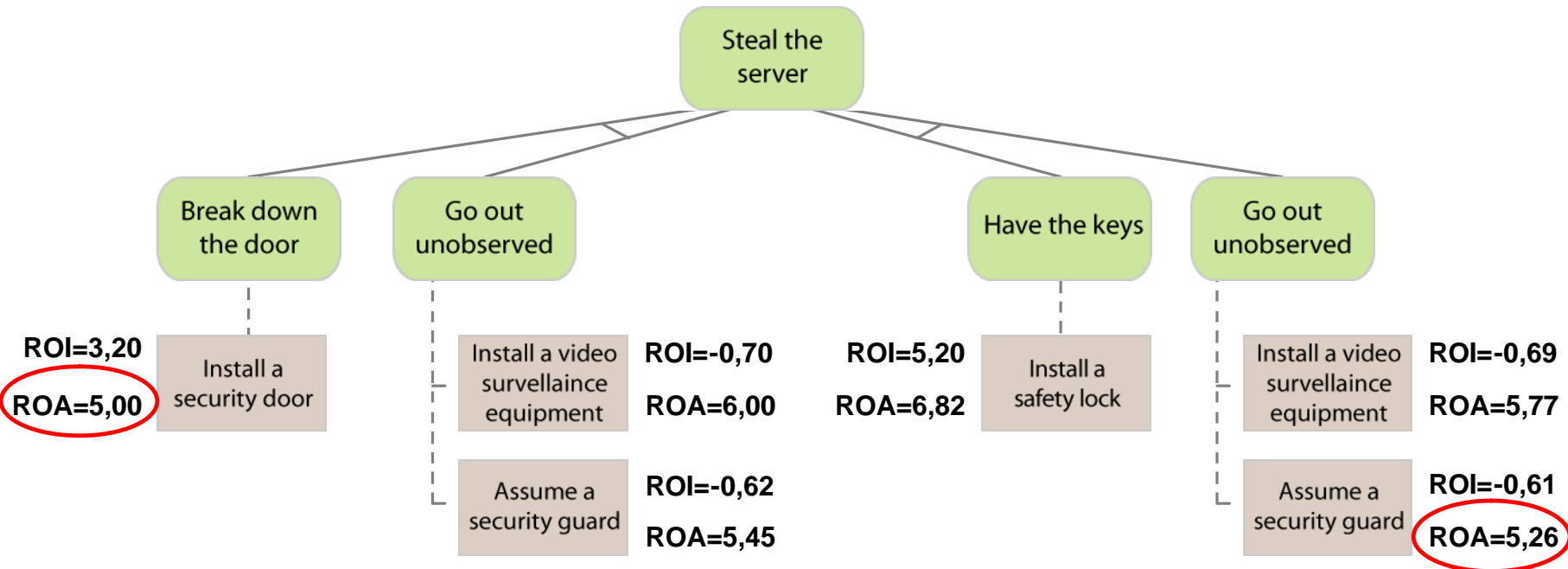
# Putting together the evaluations

+ Maximize ROI



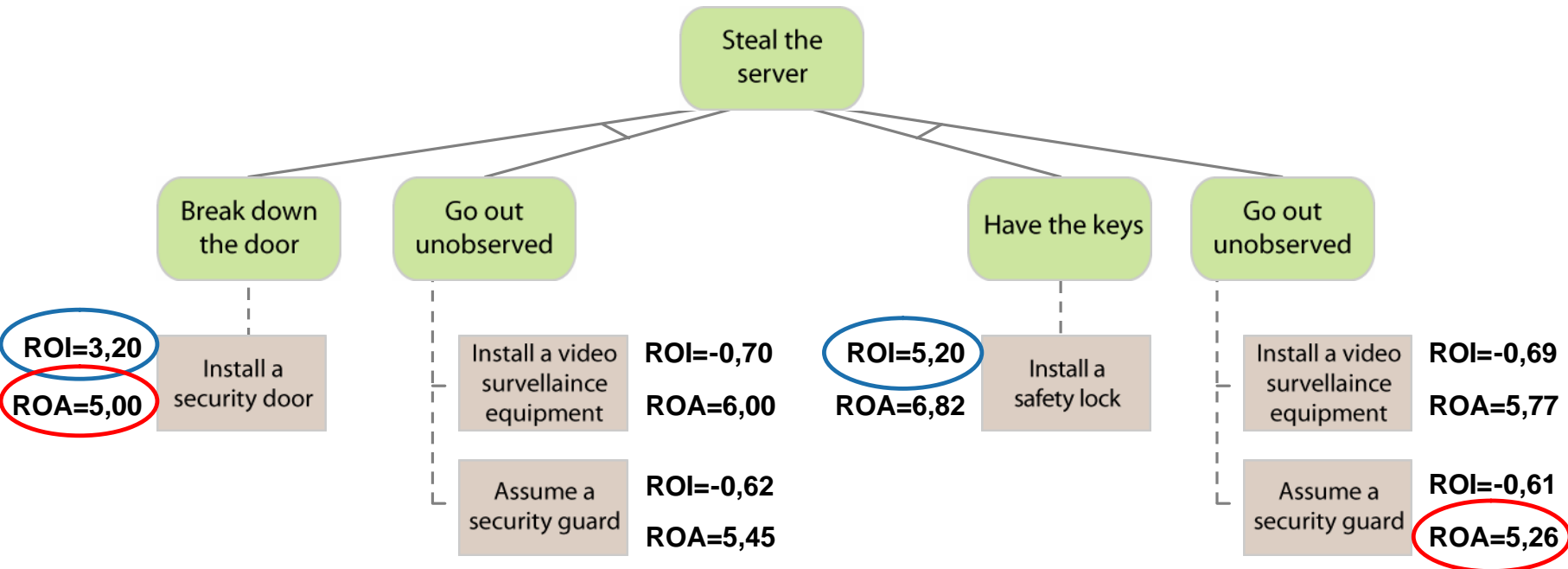
# Putting together the evaluations

+ Minimize ROA



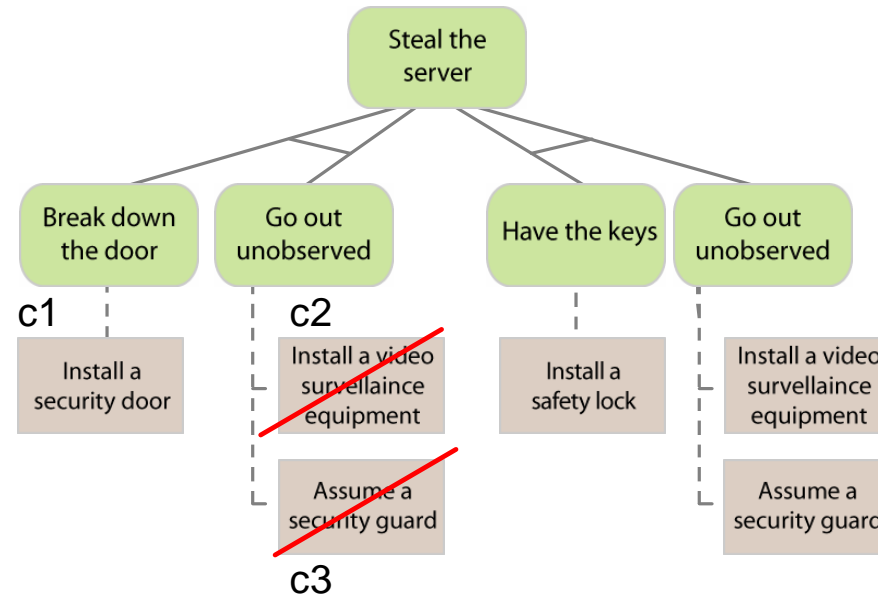
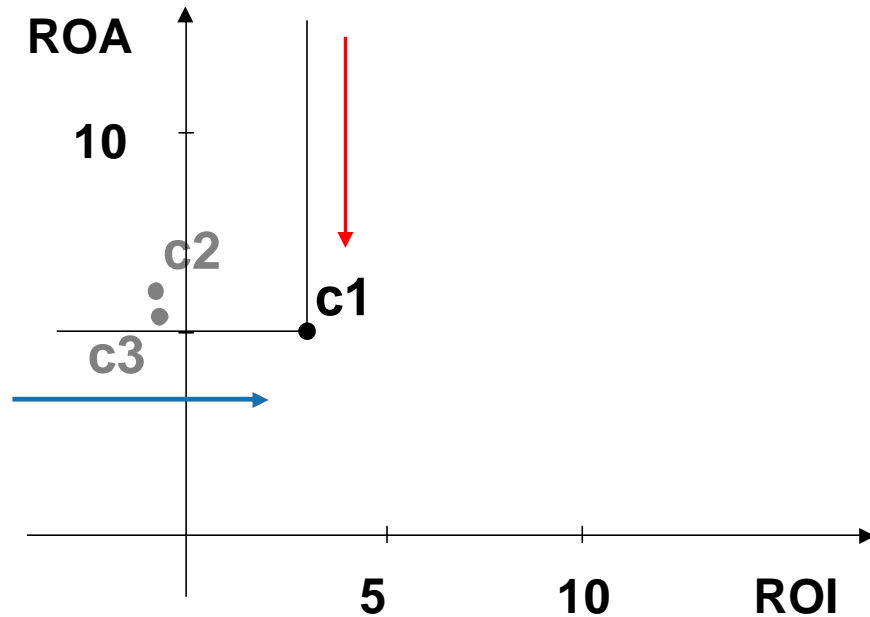
# Putting together the evaluations

+ max ROI min ROA



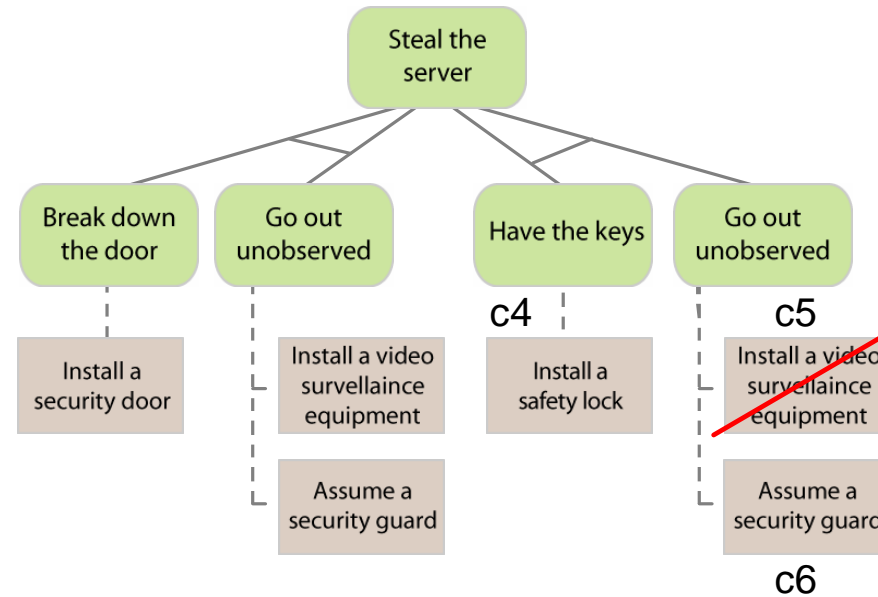
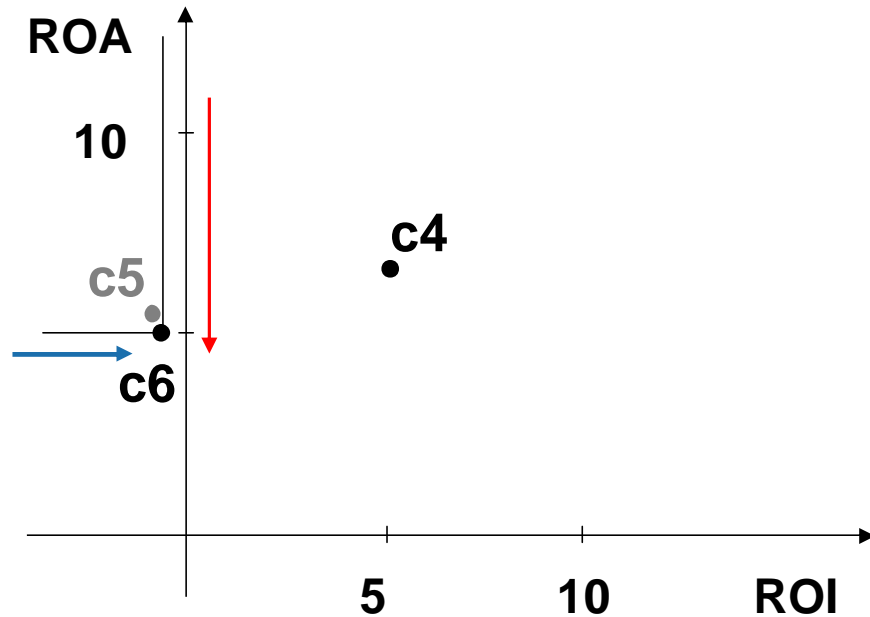
# Putting together the evaluations

The *Pareto-optimal* countermeasure for the first attack



# Putting together the evaluations

The Pareto-optimal countermeasure for the second attack

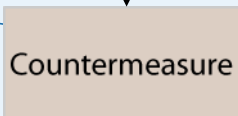
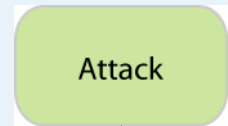




# F.W. CP-Nets

- + Relations between possibilistic logic and cp-nets
- + Uncertainties of attacks modelled as probability/possibility distribution

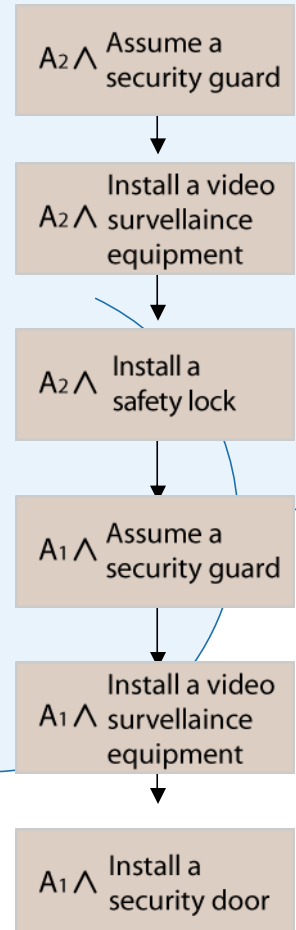
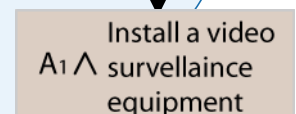
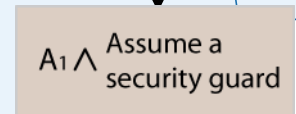
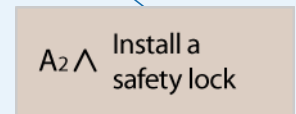
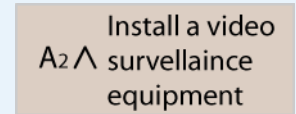
(See: CP-Net, Possibility Theory (Prade, Dubois), Uncertainty and CP-Net (?Brent Phd Thesis?))



$$A_1 \succ A_2$$

$A_1$	$C_1 \succ C_2 \succ C_3$
$A_2$	$C_4 \succ C_2 \succ C_3$

$$C_4 \succ C_1 \succ C_2 \succ C_3$$



# Conclusion and Future Work

- + From Attack to Defense trees
- + Defense trees + quantitative labels
  - + ROI
  - + ROA
- + Evaluation of multiple attacks and countermeasure
- + Heuristics to find the best configuration
  - + Minimum (cost) set cover
- + Game Theory analysis
- + *Defense Graphs*
- + Constraint intervals to represent uncertain indexes (RM, ARO, EF)