

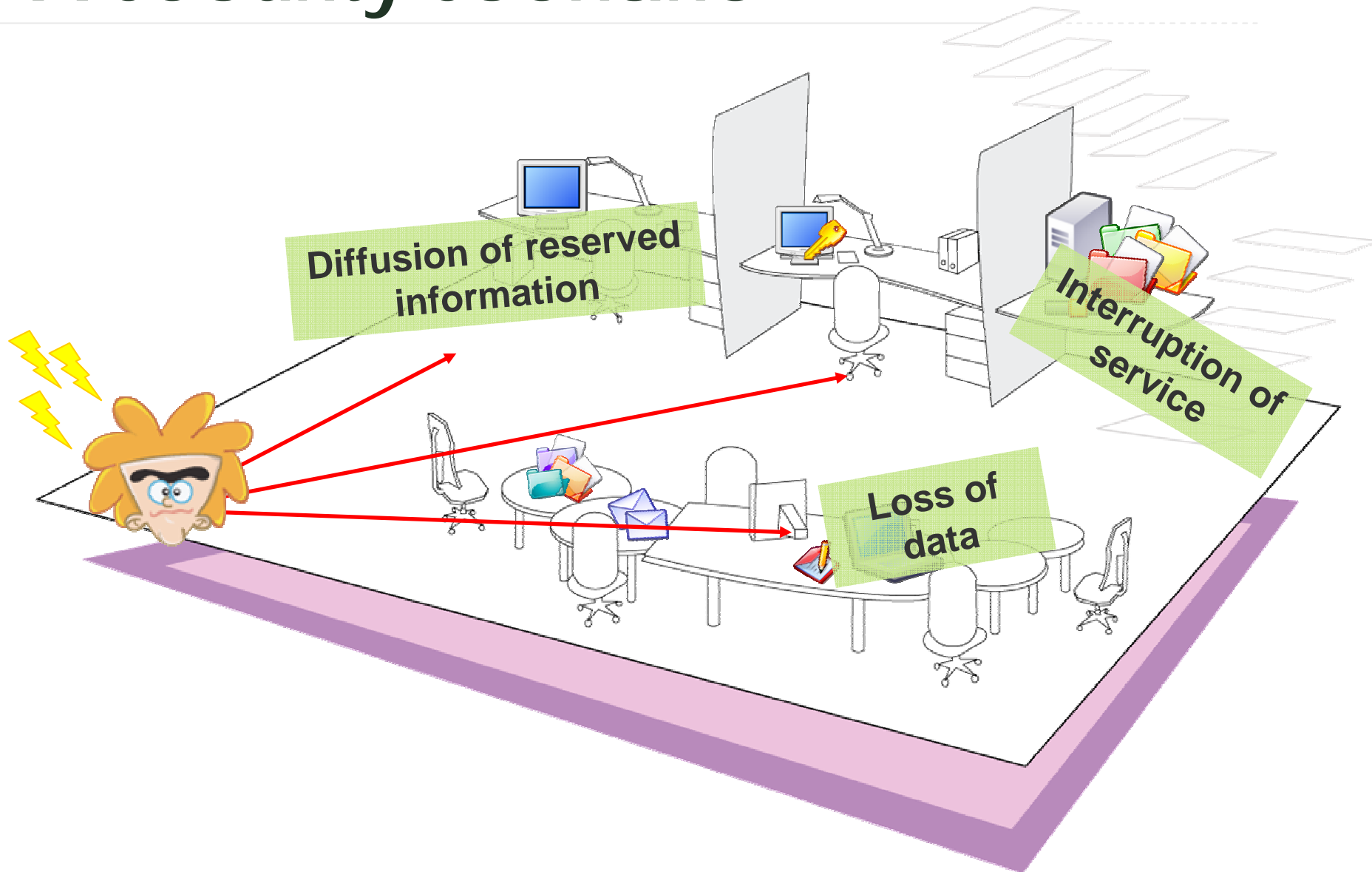
Pescara, 2 aprile 2008

Modeling and selecting preferred countermeasures using CP-nets and Answer Set Programming

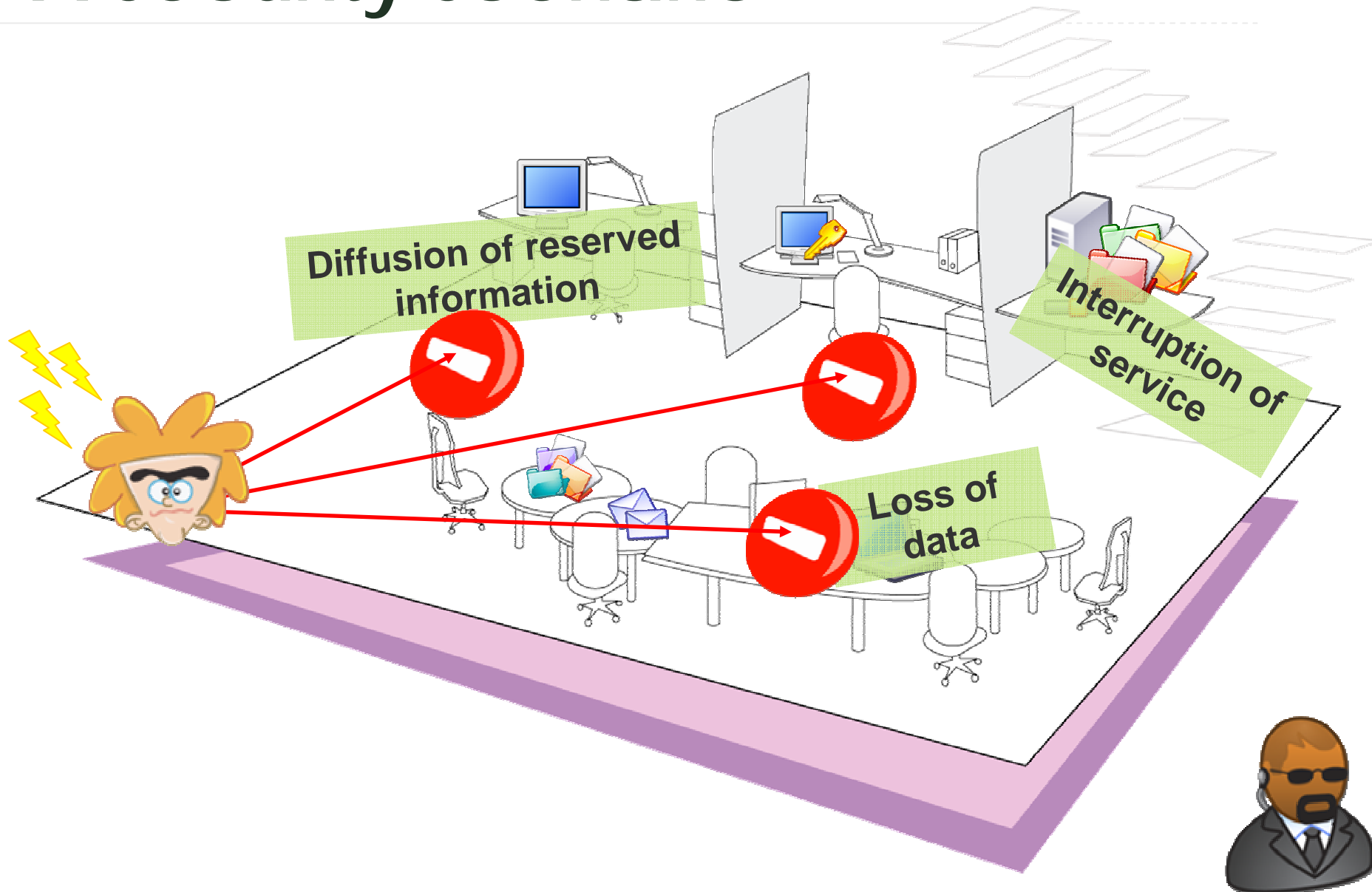
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Pescara

A security scenario



A security scenario



Agenda

- * Instruments
 - * Defence trees
 - * Cp-networks
- * CP-defence trees
 - * and-composition of attacks
 - * or-composition of attacks
- * From CP-defence trees to ASO programs:
 - * Modelling defence tree
 - * Modelling preferences among attacks and countermeasures
- * Implementation

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Defence trees

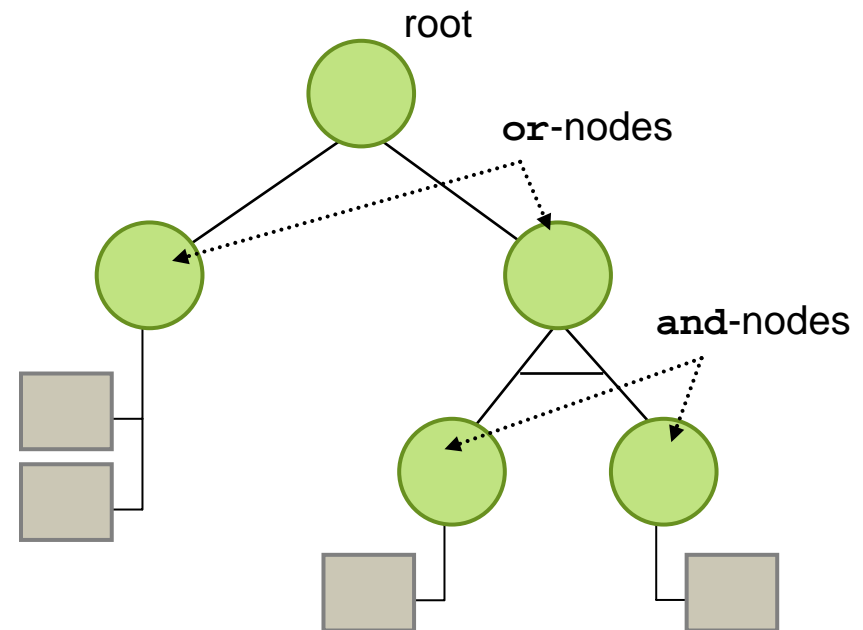
Defence trees are an extension of attack trees [Schneier00].

Attack tree:

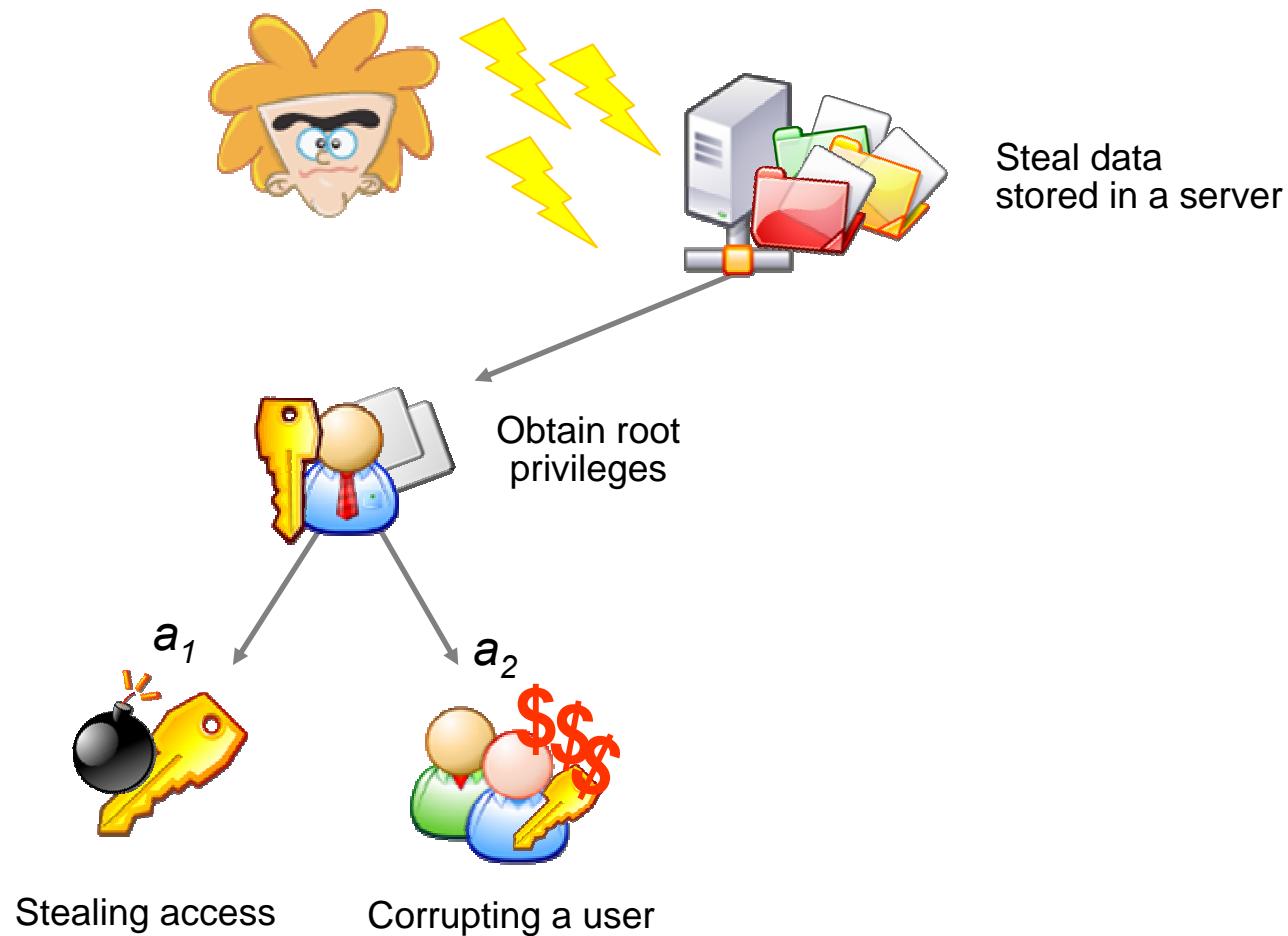
- * the root is an asset of an IT system
- * paths from a leaf to the root represent attacks to the asset
- * the non-leaf nodes can be:
 - * and-nodes
 - * or-nodes

Defence tree:

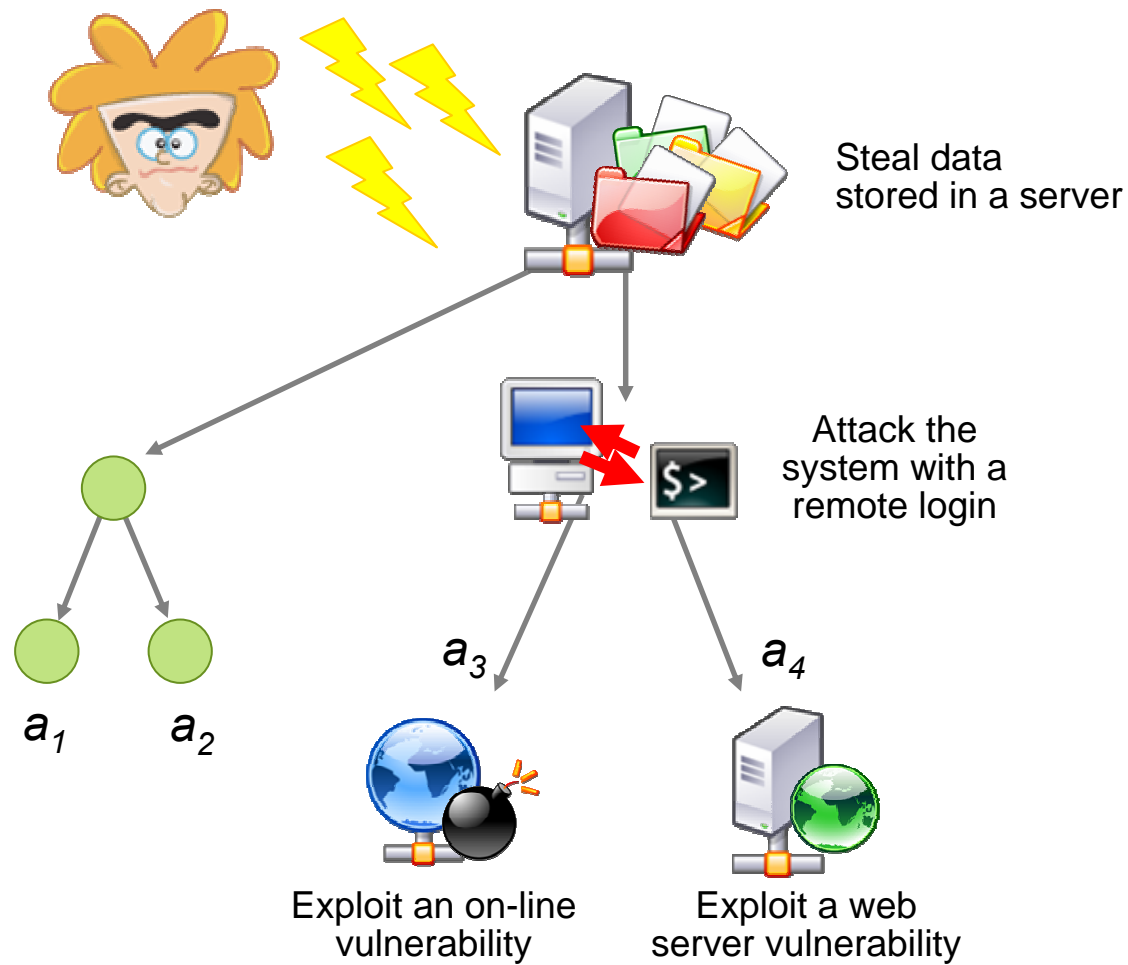
- * attack tree
- * a set of countermeasures



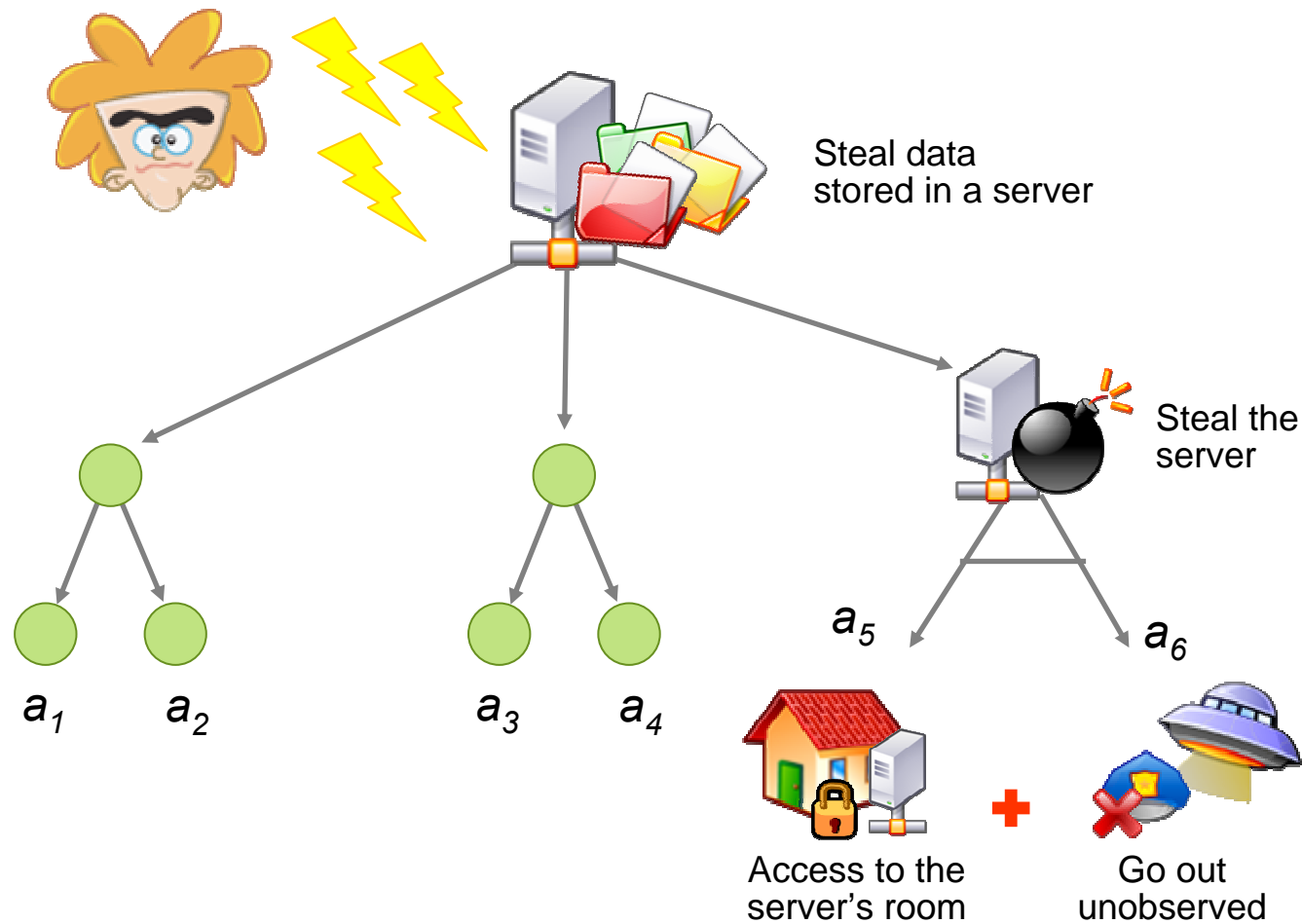
Defence trees (example)



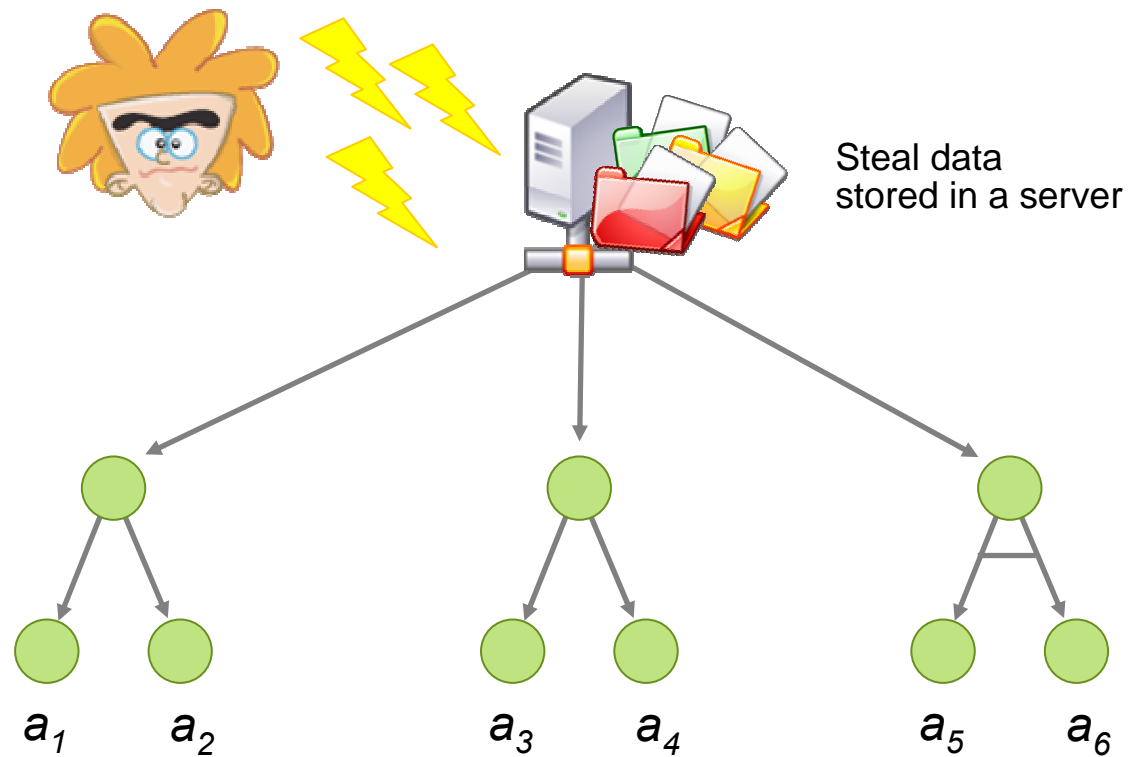
Defence trees (example)



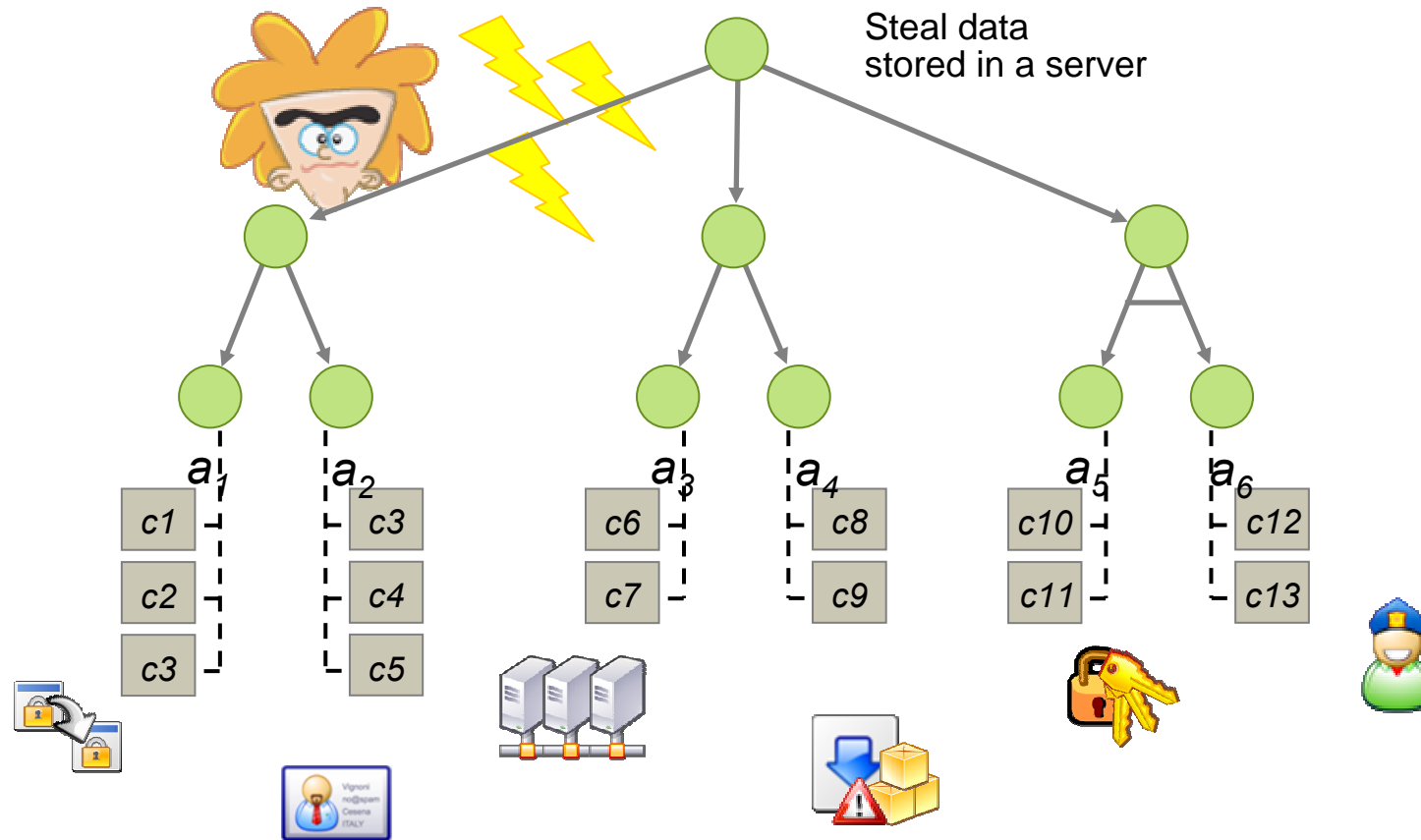
Defence trees (example)



Defence trees (example)



Defence trees (example)



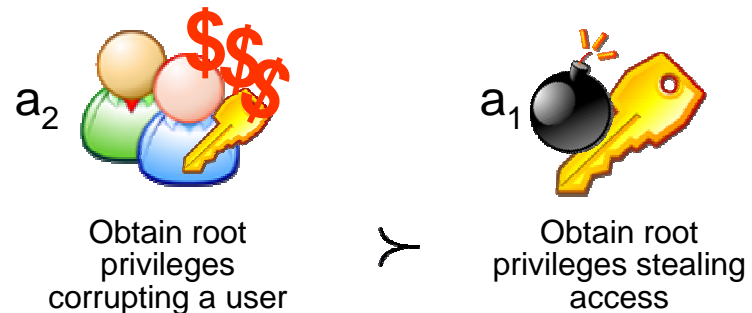
Cp-nets

Conditional preference networks [Boutiliet99] are a graphical formalism to specify and representing conditional preference relations.

- * Preferences over attack
- * Conditional preferences over countermeasures

... more dangerous than ...

$$a_2 \succ a_1$$

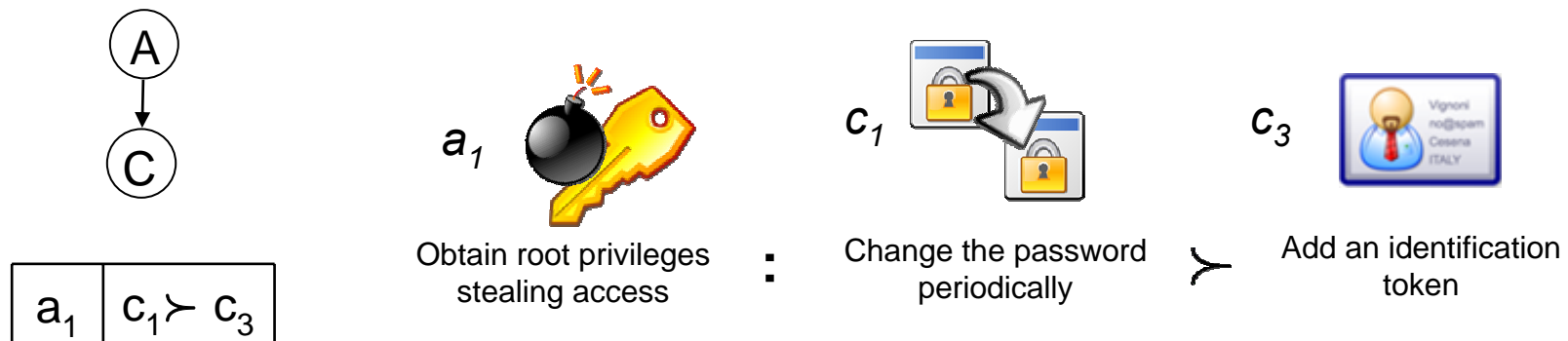


Cp-nets

Conditional preference networks [Boutiliet99] are a graphical formalism to specify and representing conditional preference relations.

- * Preferences over attack
- * Conditional preferences over countermeasures

... less expensive than ...

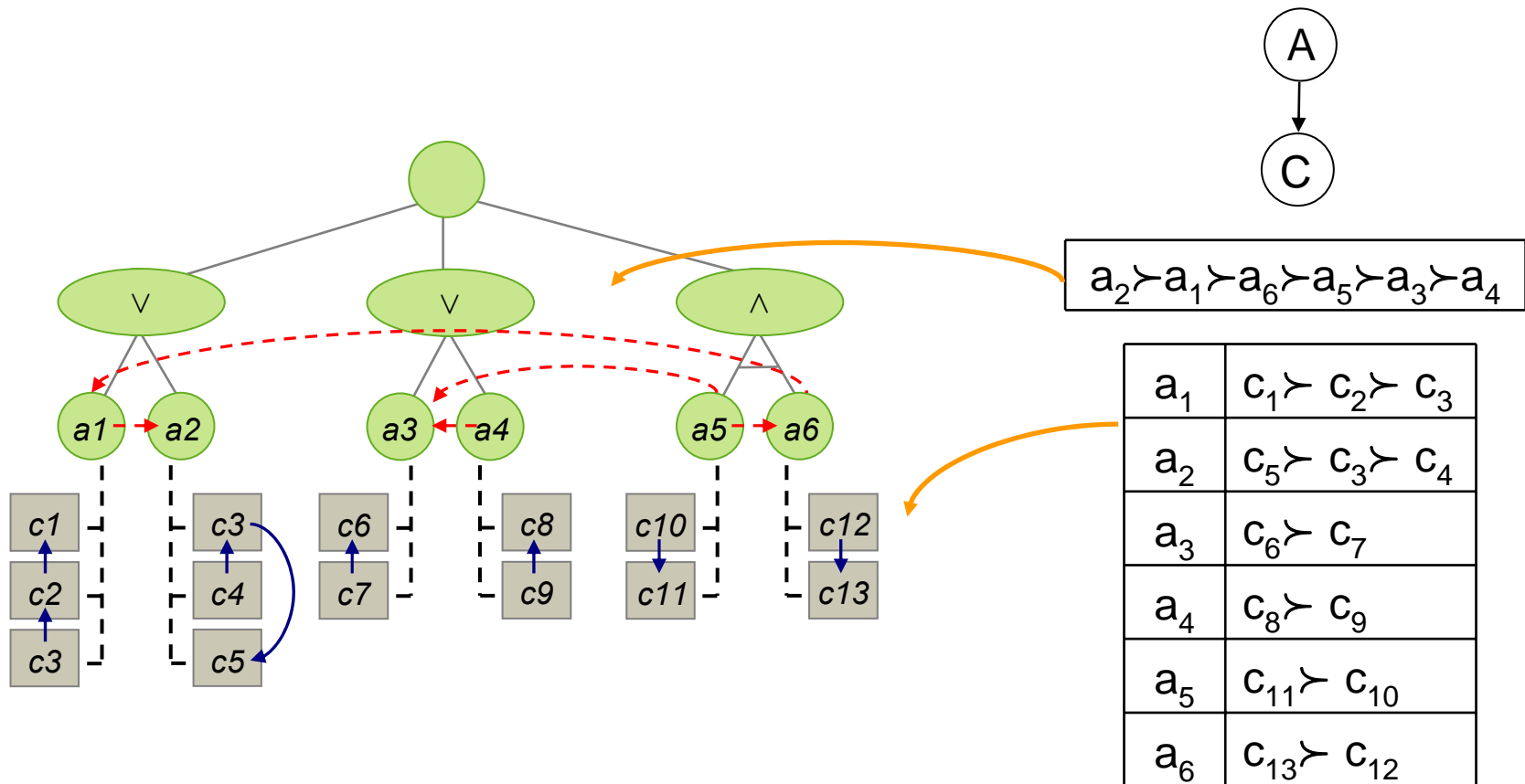


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Cp-defence tree

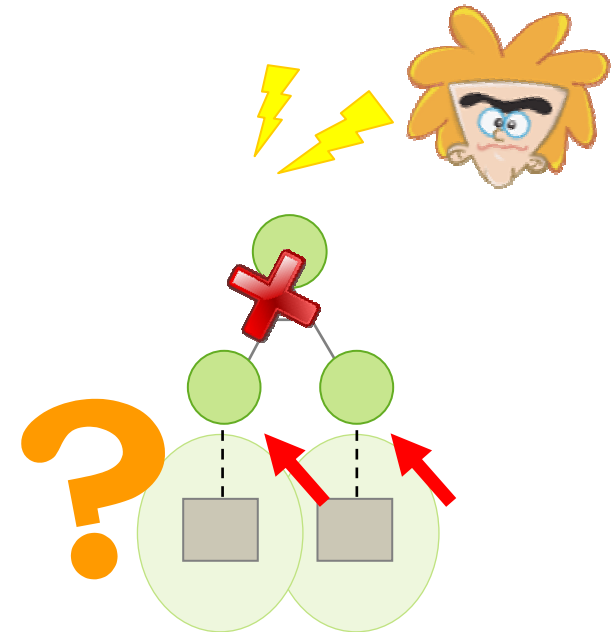
Cp-defence tree is a defence tree enriched with conditional preference over attack and countermeasures.



and-composition

An and-attack is an attack composed by a set of actions that an attacker has to successfully achieve to obtain his goal.

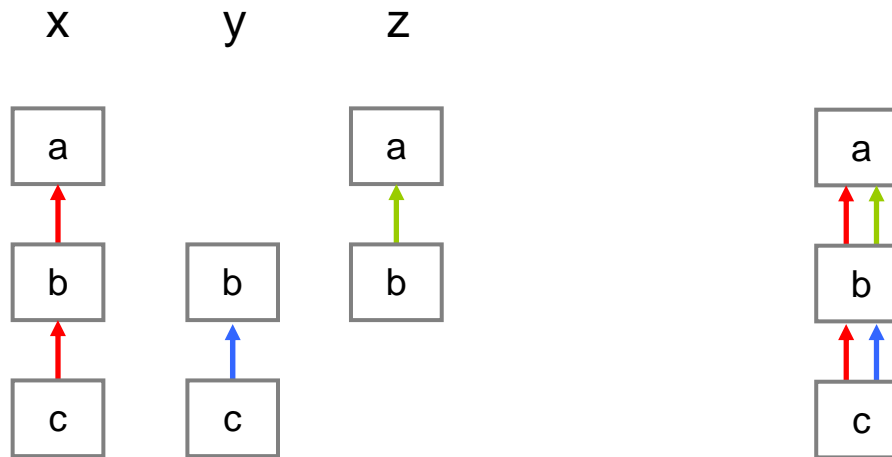
How to combine the preferences for the countermeasure associated to each attack action?



and-composition (example)

$A = \{x,y,z\}$
 $C = \{a,b,c\}$

x	$a \succ b \succ c$
y	$b \succ c$
z	$a \succ b$



$x \wedge y \wedge z : a \succ b \succ c$

and-composition

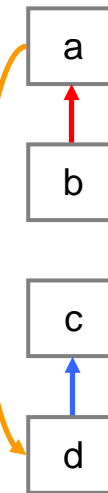
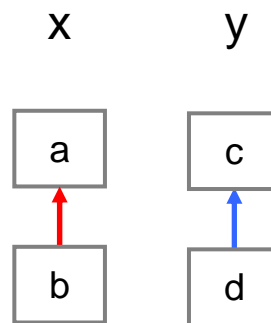
A countermeasure is preferred to another one if it is preferred in, at least, one of the partial orders.

and-composition (example 2)

$A = \{x, y\}$
 $C = \{a, b, c, d\}$

x	$a \succ b$
y	$c \succ d$

$x \succ y$



and-composition

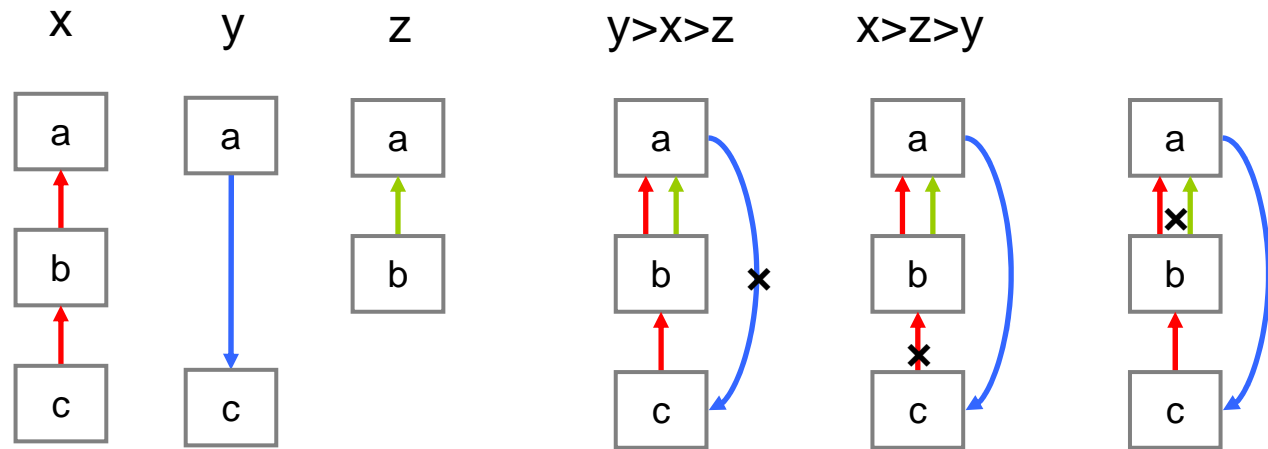
$x \wedge y : c \succ d \succ a \succ b$

We have also to consider the preferences over the value of the parent variable

and-composition: cycle

$A = \{x,y,z\}$
 $C = \{a,b,c\}$

x	a γ b γ c
y	b γ c
z	a γ b



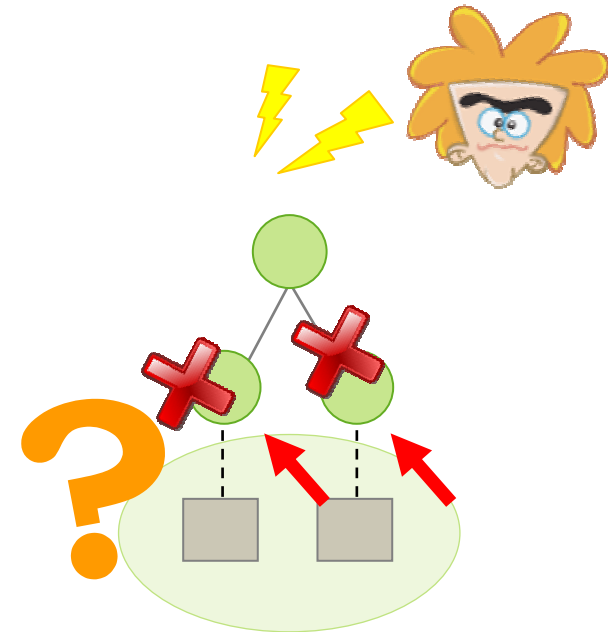
If we have any cycle we can:

- * consider the preference between the parents of the variable to delete some edge
- * use some algorithms as the Floyd's algorithm for remove cycles

or-composition

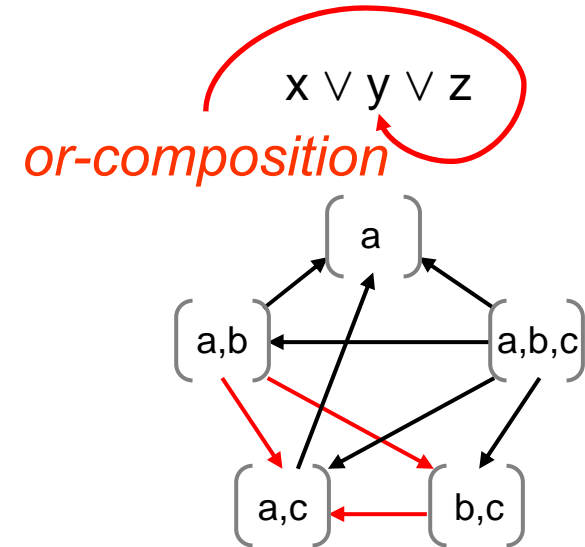
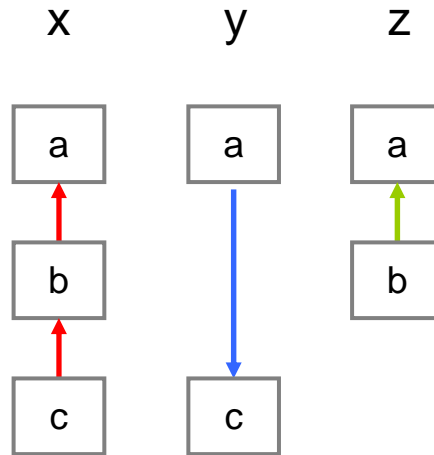
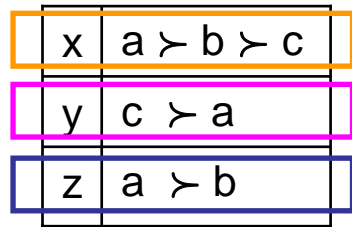
An `or`-attack is an attack that can be performed with different and alternative actions: the attacker can complete successfully any of its actions to obtain his goal

How to combine the preferences associated to each action that compose the attack and determine sets of countermeasures?



or-composition (example)

$A = \{x,y,z\}$
 $C = \{a,b,c\}$

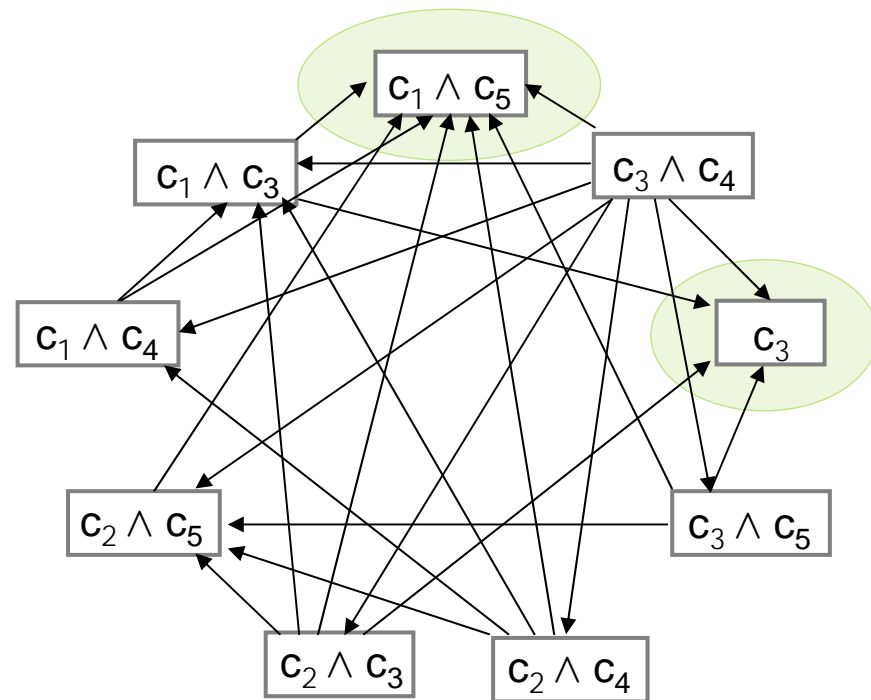
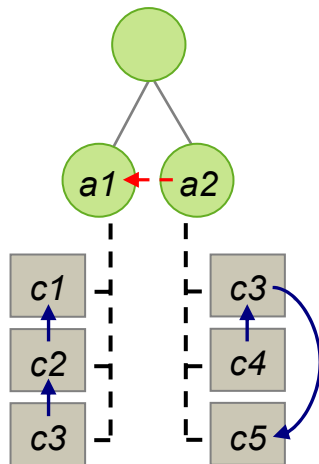


[a]	$\langle a,a,a \rangle$	$\langle a,a,b \rangle$
[a,b]	$\langle a,c,a \rangle$	$\langle a,c,b \rangle$
[a,c]	$\langle b,a,a \rangle$	$\langle b,a,b \rangle$
[b,c]	$\langle b,c,a \rangle$	$\langle b,c,b \rangle$
[a,b,c]	$\langle c,a,a \rangle$	$\langle c,a,b \rangle$
	$\langle c,c,a \rangle$	$\langle c,c,b \rangle$

$[b,c] \vee [a,b]$

or-composition: example

$a_1 \vee a_2$



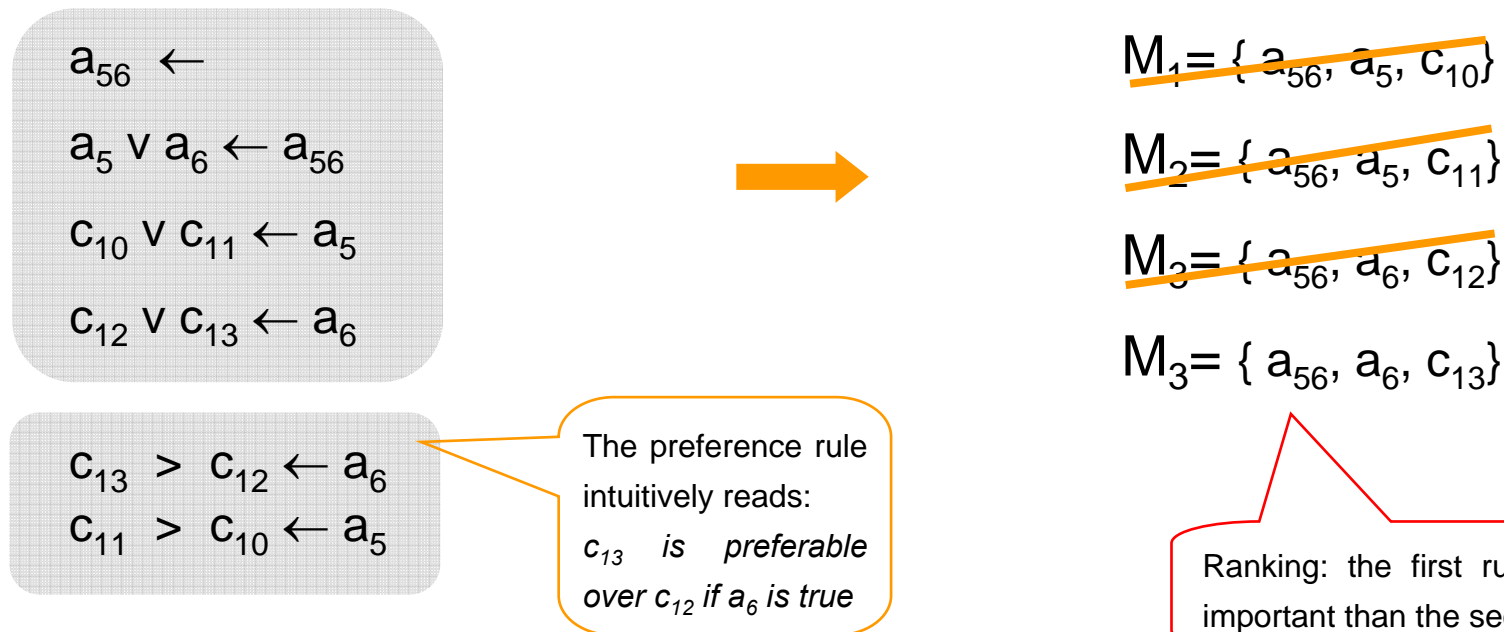
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Answer Set Optimization

An answer set optimization program $\langle P, \Phi \rangle$, where P is a logic program and Φ is a set of preference rules.

- * P defines the set of possible solutions,
- * Φ establishes the preference order among them.



and-composition

P_x $r_{x1}: x \leftarrow$

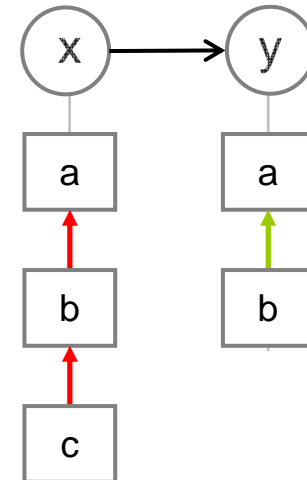
$r_{x2}: a \vee b \vee c \leftarrow x$

Φ $\rho_{x1}: a > b > c \leftarrow x$

P_y $r_{y1}: y \leftarrow$

$r_{y2}: a \vee b \leftarrow y$

Φ $\rho_{y1}: a > b \leftarrow y$



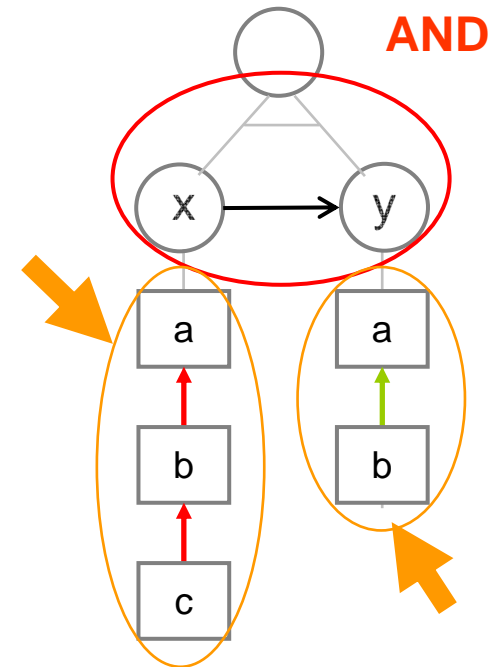
and-composition

P_x $r_{x1}: x \leftarrow$
 $r_{x2}: a \vee b \vee c \leftarrow x$
 Φ $\rho_{x1}: a > b > c \leftarrow x$

P_y $r_{y1}: y \leftarrow$
 $r_{y2}: a \vee b \leftarrow y$
 Φ $\rho_{y1}: a > b \leftarrow y$

P_{and} **AND**
 $r_1: root \leftarrow$
 $r_2: x \vee y \leftarrow root$

Φ



The optimal answer set associated to $\langle P_{and}, \Phi \rangle$ is the set $M_4 = \{root, x, a\}$
 The preferred set of countermeasures is the set $\{a\}$.

or-composition

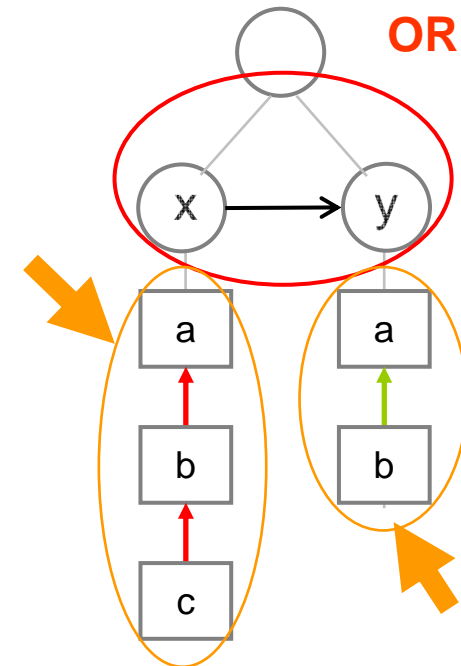
P_x $r_{x1}: x \leftarrow$
 $r_{x2}: a \vee b \vee c \leftarrow x$
 Φ $\rho_{x1}: a > b > c \leftarrow x$

P_y $r_{y1}: y \leftarrow$
 $r_{y2}: a \vee b \leftarrow y$
 Φ $\rho_{y1}: a > b \leftarrow y$

OR

P_{or} $r_1: root' \leftarrow$
 $r_2: x \leftarrow root'$
 $r_3: y \leftarrow root'$

Φ



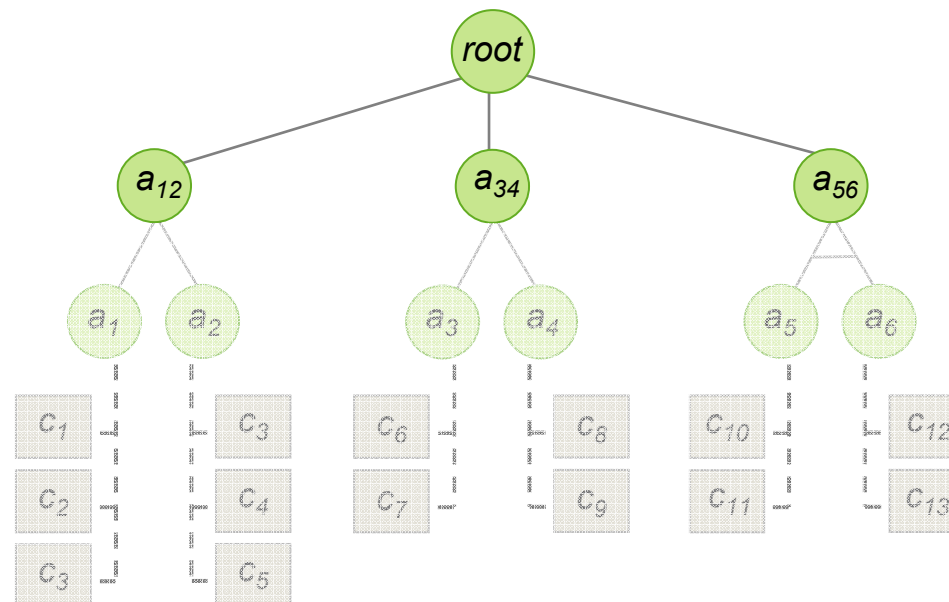
The optimal answer set associated to $\langle P_{or}, \Phi \rangle$ is $M'_1 = \{root', x, y, a\}$

The preferred set of countermeasures is the set $\{a\}$.

ASO and CP-defence tree

Logic programming

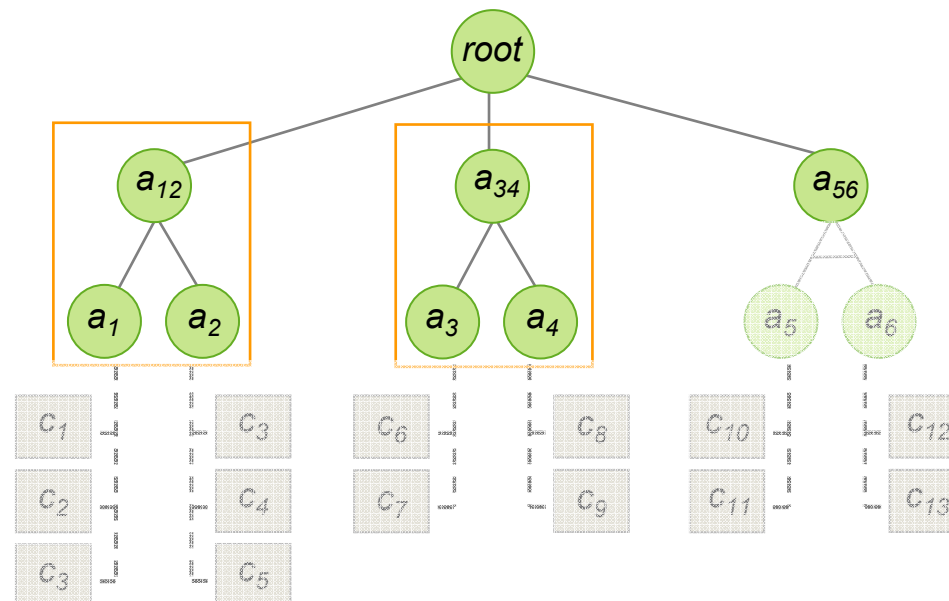
root ←
a₁₂ ← root
a₃₄ ← root
a₅₆ ← root



ASO and CP-defence tree

Logic programming

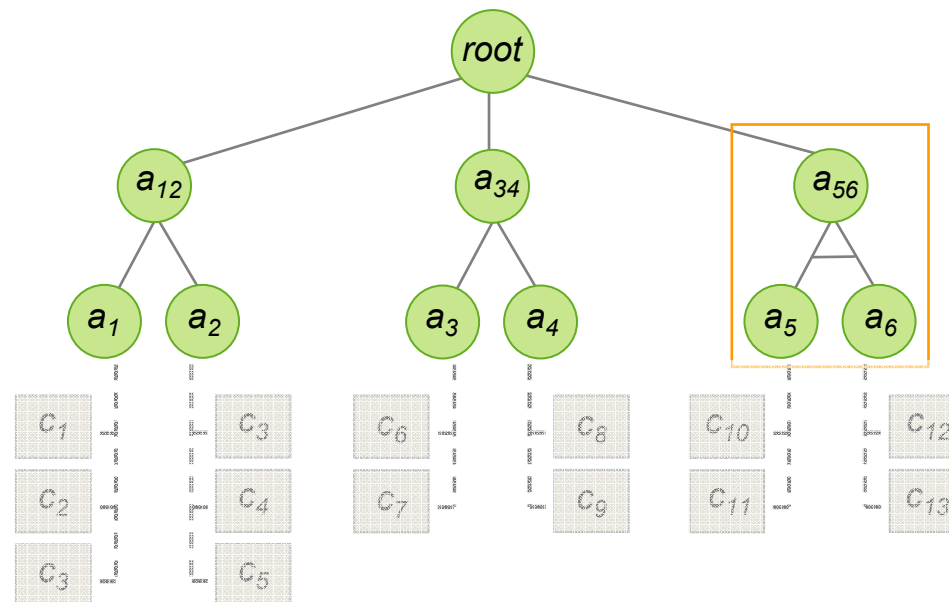
root \leftarrow
a₁₂ \leftarrow root
a₃₄ \leftarrow root
a₅₆ \leftarrow root
a₁ \leftarrow a₁₂
a₂ \leftarrow a₁₂
a₃ \leftarrow a₃₄
a₄ \leftarrow a₃₄



ASO and CP-defence tree

Logic programming

root \leftarrow
a₁₂ \leftarrow root
a₃₄ \leftarrow root
a₅₆ \leftarrow root
a₁ \leftarrow a₁₂
a₂ \leftarrow a₁₂
a₃ \leftarrow a₃₄
a₄ \leftarrow a₃₄
a₅ \vee a₆ \leftarrow a₅₆

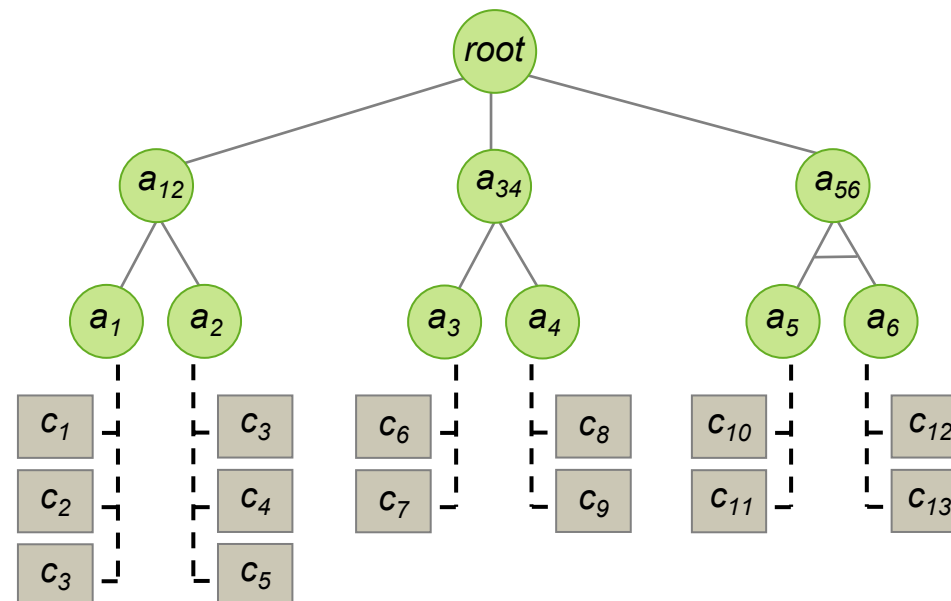


ASO and CP-defence tree

Logic programming

root \leftarrow
a₁₂ \leftarrow root
a₃₄ \leftarrow root
a₅₆ \leftarrow root
a₁ \leftarrow a₁₂
a₂ \leftarrow a₁₂
a₃ \leftarrow a₃₄
a₄ \leftarrow a₃₄
a₅ \vee a₆ \leftarrow a₅₆

c₁ \vee c₂ \vee c₃ \leftarrow a₁
c₃ \vee c₄ \vee c₅ \leftarrow a₂
c₆ \vee c₇ \leftarrow a₃
c₈ \vee c₉ \leftarrow a₄
c₁₀ \vee c₁₁ \leftarrow a₅
c₁₂ \vee c₁₃ \leftarrow a₆



ASO and CP-defence tree

Conditional preference rules

$$c_1 > c_2 > c_3 \leftarrow a_1$$

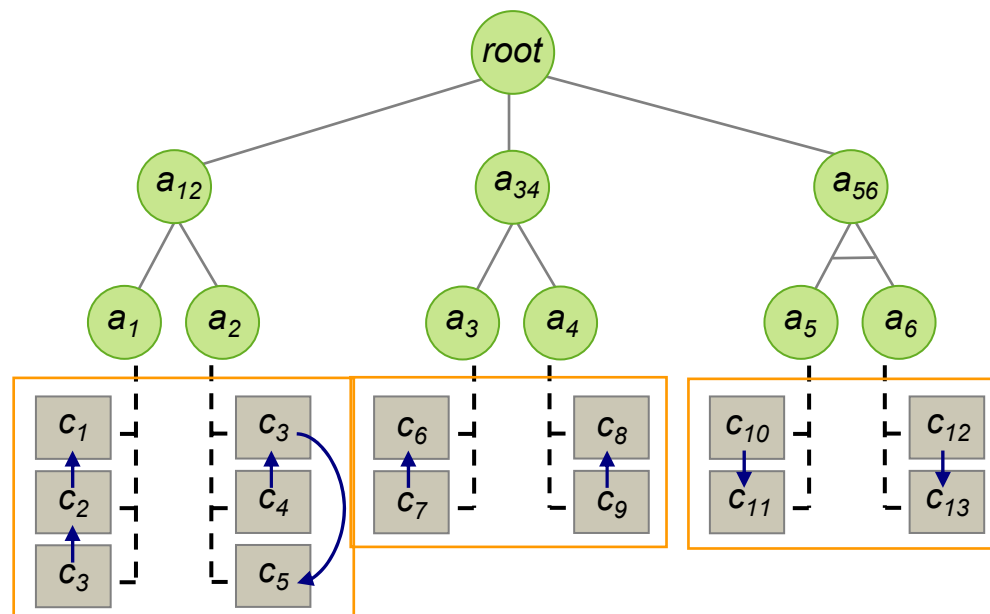
$$c_5 > c_3 > c_4 \leftarrow a_2$$

$$c_6 > c_7 \leftarrow a_3$$

$$c_8 > c_9 \leftarrow a_4$$

$$c_{11} > c_{10} \leftarrow a_5$$

$$c_{13} > c_{12} \leftarrow a_6$$



ASO and CP-defence tree

Ranking of preference rules

$$\Phi_1 \quad c_1 > c_2 > c_3 \leftarrow a_1$$

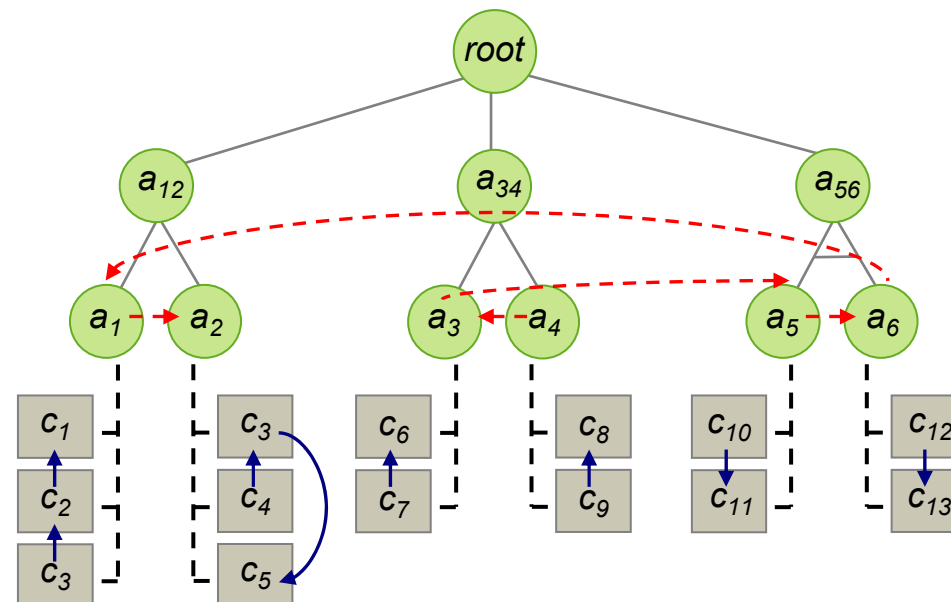
$$\Phi_2 \quad c_5 > c_3 > c_4 \leftarrow a_2$$

$$\Phi_3 \quad c_6 > c_7 \leftarrow a_3$$

$$\Phi_4 \quad c_8 > c_9 \leftarrow a_4$$

$$\Phi_5 \quad c_{11} > c_{10} \leftarrow a_5$$

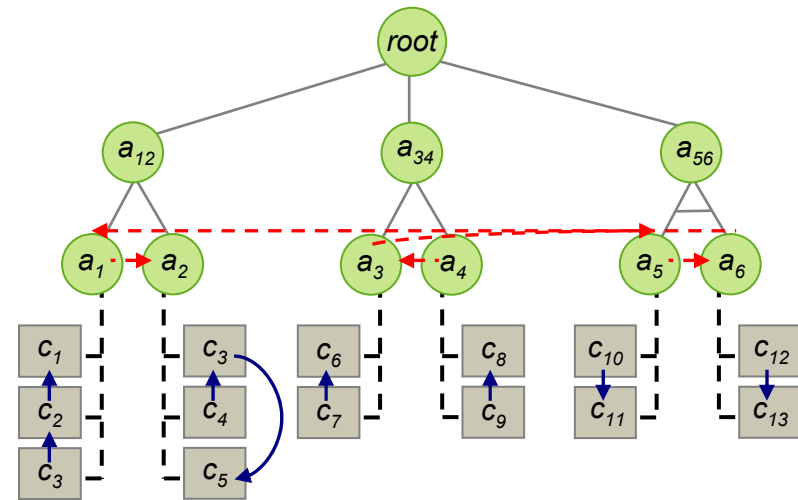
$$\Phi_6 \quad c_{13} > c_{12} \leftarrow a_6$$



ASO and CP-defence tree

$\text{root} \leftarrow$
 $a_{12} \leftarrow \text{root}$
 $a_{34} \leftarrow \text{root}$
 $a_{56} \leftarrow \text{root}$
 $a_1 \leftarrow a_{12}$
 $a_2 \leftarrow a_{12}$
 $a_3 \leftarrow a_{34}$
 $a_4 \leftarrow a_{34}$
 $a_5 \vee a_6 \leftarrow a_{56}$

$c_1 \vee c_2 \vee c_3 \leftarrow a_1$
 $c_3 \vee c_4 \vee c_5 \leftarrow a_2$
 $c_6 \vee c_7 \leftarrow a_3$
 $c_8 \vee c_9 \leftarrow a_4$
 $c_{10} \vee c_{11} \leftarrow a_5$
 $c_{12} \vee c_{13} \leftarrow a_6$



$\Phi_1 \quad c_5 > c_3 > c_4 \leftarrow a_2$
 $\Phi_2 \quad c_1 > c_2 > c_3 \leftarrow a_1$
 $\Phi_3 \quad c_{13} > c_{12} \leftarrow a_6$
 $\Phi_4 \quad c_{11} > c_{10} \leftarrow a_5$
 $\Phi_5 \quad c_6 > c_7 \leftarrow a_3$
 $\Phi_6 \quad c_8 > c_9 \leftarrow a_4$

$M = \{ \text{root}, a_{12}, a_{34}, a_{56}, a_1, a_2, a_3, a_4, c_1, c_5, c_6, c_8, a_6, c_{13} \}$
 $\uparrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow$

Best set of countermeasures: $\{c_1, c_5, c_6, c_8, c_{13}\}$

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Implementation

